# A Novel Hybrid Method based on Krill Herd and Cuckoo Search for Optimal Power Flow Problem

Aboubakr Khelifi<sup>1\*</sup>, Bachir Bentouati<sup>1</sup>, Saliha Chettih<sup>1</sup>, Ragab A. El-Sehiemy<sup>2</sup>

<sup>1</sup> Electrical Engineering Department, LMSF Laboratory, Amar Telidji University of Laghouat, Algeria <sup>2</sup> Electrical Engineering Department, Faculty of Engineering-Kafrelsheikh University, Egypt <sup>1</sup> Email: a.khelifi@lagh-univ.dz; b.bentouati@lagh-univ.dz; s.chettih@lagh-univ.dz. <sup>2</sup> Email: elsehiemy@eng.kfs.edu.eg;

Received: 24 October 2018; Accepted: 07 August 2019; Published: 08 September 2019

Abstract-Solving the Optimal power flow (OPF) problem is an urgent task for power system operators. It aims at finding the control variables' optimal scheduling subjected to several operational constraints to achieve certain economic, technical and environmental benefits. The OPF problem is mathematically expressed as a nonlinear optimization problem with contradictory objectives and subordinated to both constraints of equality and inequality. In this work, a new hybrid optimization technique, that integrates the merits of cuckoo search (CS) optimizer, is proposed to ameliorate the krill herd algorithm (KHA)'s poor efficiency. The proposed hybrid CS-KHA has been expanded for solving for single and multi-objective frameworks of the OPF problem through 11 case studies. The studied cases reflect various economic, technical and environmental requirements. These cases involve the following objectives: minimization of non- smooth generating fuel cost with valve-point loading effects, emission reduction, voltage stability enhancement and voltage profile improvement. The CS-KHA presents krill updating (KU) and krill abandoning (KA) operator derived from cuckoo search (CS) amid the procedure when the krill updating in order to extraordinarily improve its adequacy and dependability managing OPF problem. The viability of these improvements is examined on IEEE 30-bus, IEEE 57-bus and IEEE 118-bus test system. The experimental results prove the greatest ability of the proposed hybrid meta-heuristic CS-KHA compared to other famous methods.

*Index Terms*—Cuckoo search algorithm (CS); krill herd algorithm (KHA); optimal power flow (OPF); voltage stability (VS); valve-point effect; emission reduction.

## I. INTRODUCTION

The problem of optimal power flow (OPF) is significated considerable attention in recent years and has based its position among the main tools for the operation and planning of recent power systems. OPF is a nonlinear programming problem. The major objective is to find the correct adjustment of its control variables that optimize specific objective functions/functions while sufficient the operational constraints of equality and inequality at specified loading settings and defined system parameters [1-3].

The OPF has been applied to regulate the production of real powers, generators terminal voltages, setting of transformer taps, shunt reactors/capacitors and other control variables to improve the power system requirements by minimizing the production fuel costs, reducing the network active power losses, enhance the voltage stability and voltage profile at load buses. The previous requirements are achieved while all operational requirements are preserved within the accepted operation limitations as The voltages of load bus, the reactive power products of the generator, the network's power flows and whole other state variables in the power system within their assure and operational bounds.

In its most popular formulation, the OPF is static, a non-convex, wide-ranging optimization problem with both discontinuous and continuous control variables. Even in operating cost functions' absence of non-convex generators, prohibited operating zones (POZ) of generating units and discontinuous control variables, the OPF problem is a non-convex because of the presence of non-linear alternating current power flow equality constraints. The existence of discontinuous control variables, like transformer tap positions, phase shifters, switchable shunt devices, added more difficulty the formulation and solution of the problem.

The methods were evolving to solve OPF problem can be categorized into two types conventional and advanced optimization techniques. The traditional optimization techniques were used derivatives and gradient operators. These techniques are usually not capable to find or determine the global optimal. Several mathematical suppositions like analytic, convex and differential objective functions must be made to simplicity the problem. Nevertheless, the OPF's problem is a problem of optimization non-convex and non-smooth objective function in general. As a result, it is significant to evolve optimization methods that are effective in dominating these disadvantages and to treat this hardness effectively. The computational materials' evolution in recent decades has motivated to the development of advanced optimization methods that were so-called meta-heuristics.



These techniques can dominate many disadvantages of conventional techniques [4]. Several of these recent techniques have been applied to solve the OPF problem like: Simulated Annealing (SA) [5], Genetic Algorithm (GA) [6,7], Differential Evolution (DE) [8], Tabu Search (TS) [9], Imperialist Competitive Algorithm (ICA) [10], Particle Swarm Optimization (PSO) [11], adaptive real coded biogeography-based optimization (ARCBBO)[12], Biogeography Based Optimization (BBO) [13,14], multiphase search algorithm [15], Gbest guided artificial bee colony algorithm(Gbest-ABC) [16], Gravitational Search Algorithm (GSA) [17], Artificial Bee Colony (ABC) Optimizer Multi-objective Grey Wolf [18], (MOGWO)[19], black-hole-based optimization (BHBO) [20], Teaching Learning based Optimization (TLBO) [21], Sine-Cosine Optimization algorithm (SCOA) [22], Group Search Optimization (GSO) [23], hybrid algorithm of particle swarm optimizer with grey wolves(PSO-GWO) [24], quasi-oppositional teaching-learning based optimization [31]have been incorporated into it. state-of-the-art Meanwhile, many meta-heuristic techniques, like Improved Colliding Bodies Optimization (ICBO) [32], Moth Swarm Algorithm (MSA) [33], Moth-Flame Optimization (MFO) [34], cuckoo search [35], firefly algorithm [36] and Backtracking Search Optimization Algorithm (BSA) [37] Surveys of different meta-heuristics used to solve the problem of OPF are offered in[25] The applications of these methods on different size systems lead to competitive results and therefore were favorable and encouraging for more study in this trend. Furthermore, because of the objectives' contrast where various functions can be envisaged for modeling the OPF problem, of course not technique can be seen as the preferable in solving whole OPF problems. Hence, it is constantly needed to have a novel technique that can successfully solve several of the OPF problems.

Optimization is turning a area of request to analysts, particularly since a framework's the competence depends on obtaining an arrangement an order that can be acquired through suitable optimization technique. It is a method in order to discover the perfect solution next assessing the cost function that denotes the association among the system framework and its limitations. Presently, meta-heuristic algorithms are being formed in many regions for example crossbreeding, multi-objective type, binary type, preparing multi-layer perceptron and ways as L évy flight, operator, and chaos theory. Most of these improvements happened because the deterministic and evolutionary components are used [23]. A perfect incorporation of global and local search has intensive local exploration and global exploration [25].

Krill herd method (KH) first suggested by Gandomi and Alavi in 2012 [26] and because it performs well, many optimization strategies such as chaotic theory [27, 28, 36], Flower Pollination Algorithm (FPA) [29] and colonial competitive differential evolution (CCDE)[30] have been hybridized with the fundamental KH algorithm as mutation operator with the objective of further enhancing the performance of KHA. Furthermore, to make KHA perform in the most ideal way, a parametric study has been conducted through an array of standard benchmark functions [38].

Furthermore, KHA is a new population-build swarm computation [26] in view of the Lagrangian and revolutionary conduct of krill people in wildlife for utilization and investigation in a problem of optimization. KH computation occasionally is not able to must avoid local optimum [27] and [28].

Firstly, as portrayed here, a successful hybrid Meta heuristic cuckoo search krill herd (CS-KHA) technique in light of KHA and CS is initially suggested to accelerate convergence. In CSKH, we use an essential KHA to select an encouraging solution set. Consequently, krill updating (KU) and krill abandoning (KA) operator started from CS algorithm are added to the method. The KU operator is to a decent encouraging arrangement; while KA operator is made use of further improving the investigation of the CS-KHA to substitute the worse krill's a small amount at the finale of every generation.

The performance of this approach is utilized to keep away from local optimum and obtain a worldwide ideal solution, in addition, minimal computational time to achieve the ideal solution, local minimum evasion, and quicker convergence, which produce them suitable for viable implementations for solving various constrained optimization problems. The purpose of this article is to develop an improved KHA called CS-KHA to solve OPF problem. So as to proven the evolution of the CS-KHA, its efficiencies are compared to CS, KHA and other wellknown optimization methods.

The rest of article is structured in the next form: The following segment outlines the formulation of the OPF problem; meanwhile, section 3 depicts the algebraic equation of CS-KHA. Section 4 shows the simulation's results and discussion. While the finally conclusion of this paper is in section 5.

#### II. FORMULATION OF OPTIMAL POWER FLOW (OPF)

The problem of OPF aims at finding the control variables' optimal setting through minimizing /maximizing a predefined objective function while a collection of equality and inequality constraints satisfied. OPF considering the system's operating limit, hence it can be defined like a non-linear constrained optimization problem.

$$Minimize: f(x, u) \tag{1}$$

Subject to:

$$h(x,u) = 0$$
  
$$g(x,u) \le 0$$
 (2)

Where, u is the independent variable or control's vector, is the dependent variables or state's vector. Objective functions of OPF, g(x, u): set of inequality constraints, h(x, u): set of equality constraints.

#### A. Control variables

The vector of power network control variables is expressed as follows [37]:

$$u = \left[P_{G_2} \cdots P_{G_{NG}}, V_{G_1} \cdots V_{G_{NG}}, Q_{C_1} \cdots Q_{C_{NC}}, T_1 \cdots T_{NT}\right] \quad (3)$$

Where,  $P_{G_i}$  is the *i*-th active power bus generator. Chosen from bus 1 as swing bus is represented just and any one of the generator buses can be swing bus.  $V_{G_i}$  is the voltage magnitude at *i*-th voltage controlled generator bus, Tj is the *j*-th branch transformer tap, QCk is the shunt compensation at *k* th bus NG NC and are the

shunt compensation at *k*-th bus. *NG*, *NC* and are the generators' number, transformers and shunt VAR compensators. Any value within its range can be assumed as a control variable. Practically, transformer taps are not constant. Be that as it may, the tap settings indicated are in p.u. and outright voltage's estimation is not represented. Subsequently, for the aim of this study and to compare with previously described results, all control variables including tap settings are viewed constant for general cases of study.

## B. State (dependent) variables

The power system's state variables can be expressed through vector x as:

$$x = \left[ P_{G_1}, V_{L_1} \dots V_{L_{NL}}, Q_{G_1} \dots Q_{G_{NG}}, S_{l_1} \dots S_{l_{nl}} \right]$$
(4)

where,  $P_{G_i}$  is the active power of generator at slack bus,  $Q_{G_i}$  is the generator's reactive power linked to bus *i*, is the *p*-th load bus's bus voltage (PQ bus) and *q*-th line's line loading of is specified by. *NL* and *nl* are the load buses' number and lines of transmission respectively[40].

## C. Power System Constraints

As aforesaid earlier, the problem of OPF presents both operational constraints on equality and inequality. These constraints are defined as follows:

## C.1. Equality constraints

In OPF, the reactive and real power equilibrium equations are represented the system constraints of equality are formulated as for all system buses:

$$P_{G_i} - P_{D_i} - V_i \sum_{j=1}^{NB} V_j \left[ G_{ij} \cos\left(\delta_{ij}\right) + B_{ij} \sin\left(\delta_{ij}\right) \right] = 0 \quad (5)$$

$$Q_{G_i} - Q_{D_i} - V_i \sum_{j=1}^{NB} V_j \left[ G_{ij} \sin\left(\delta_{ij}\right) + B_{ij} \cos\left(\delta_{ij}\right) \right] = 0 \quad (6)$$

Where,  $\delta_{ij} = \delta_i - \delta_j$  is the voltage angles among bus *i* and bus *j*, NB is the buses' number,  $Q_{Di}$  and  $P_{Di}$  are reactive and real load demands.  $G_{ij}$  is the transfer

conductance and  $B_{ij}$  is the susceptance among bus *i* and bus *j*, respectively.

## C.2. Inequality constraints

The inequality's constraint in the OPF reflects the equipment's operating limit in the power system, and too reflects the limitation of the line and the load bus to ensure the safety of the system.

a) Generator constraints:

$$V_{G_i}^{\min} \leq V_{G_i} \leq V_{G_i}^{\max} \forall i \in NG$$
(7)

$$P_{G_i}^{\min} \le P_{G_i} \le P_{G_i}^{\max} \forall i \in NG$$
(8)

$$Q_{G_i}^{\min} \le Q_{G_i} \le Q_{G_i}^{\max} \forall i \in NG$$
(9)

b) Transformer constraints:

$$T_{j}^{\min} \leq T_{j} \leq T_{j}^{\max} \forall j \in NT$$
(10)

c) Shunt compensator constraints:

$$Q_{C_k}^{\min} \le Q_{C_k} \le Q_{C_k}^{\max} \forall k \in NC$$
(11)

d) Security constraints:

$$V_{L_p}^{\min} \le V_{L_p} \le V_{L_p}^{\max} \forall p \in NL$$
(12)

$$S_{l_q} \leq S_{l_q}^{\max} \forall q \in nl$$
 (13)

The control variables in constraints of inequality are self-limiting. The technique of optimization chooses a viable value for every like variable within the determined scope. Efficient methods for dealing with constraints of inequality related to dependent or state variables.

#### **III. SUGGESTED HYBRID TECHNIQUE**

## A. KH technique

The KH technique is built on the natural inspiration of conduct krill individuals' imitation in the krill population. The KH technique is motivated by krill activities like [26]: 1/The movement of other krill individuals is induced; 2/Food search activity; 3/random scattering. The optimization technique has the ability to search for an uncertain search space.

• Lagrangian model is extended to an n-dimensional decision space:

$$\frac{dX_k}{dt} = N_k + F_k + D_k \tag{14}$$

Where  $N_k$  the movement is stimulated by other members of the krill;  $F_k$  is the feeding movement and  $D_k$  is the physical diffusion of the  $k_{th}$  krill.

The movement stimulated expresses the conservation of density through every individual. The matimatical formula reflects this conduct, which is worded as follows:

$$N_{k}^{next} = N^{\max} \alpha_{k} + \omega_{d} N_{k}^{present}$$
(15)

$$\alpha_k = \alpha_k^{local} + \alpha_k^{t \operatorname{arget}}$$
(16)

Wherein  $N^{\max}$  is the highest stimulated velocity,  $\omega_d$  indicates the inertia weight in [0, 1],  $N_k^{\text{Ancient}}$  is the preceding movement  $\alpha_k^{local}$  and  $\alpha_k^{target}$  indicate the local effect of the neighbor, which is the best solution of the  $k_{th}$  individual.  $\alpha_k^{target}$  is formulated by the following equations:

$$\alpha_{k}^{t \operatorname{arget}} = C^{best} \stackrel{\wedge}{K}_{k, best} \stackrel{\wedge}{X}_{k, best}$$
(17)

$$C^{best} = 2\left(r_1 + \frac{I}{I_{\max}}\right) \tag{18}$$

where,  $C^{best}$  is the krill individual's effective coefficient with the preferable fitness for the first  $k_{th}$  krill,  $\hat{K}_{k,worst}$ and  $\hat{K}_{k,best}$  are the worst and preferable krill's fitness value so far; is a random values' number among 0 and 1. It is used to improve exploration, I is the current iterations' number, and  $I_{max}$  is the iterations' maximum number.

Foraging activities/movements are mathematically calculated as follows:

The foraging action consists of two major parameters. Premier is the position of the food  $F_k^{next}$ , followed by the preceding experiment  $\beta_k$  around the position of the food.

$$F_k^{next} = V_f \beta_k + \omega_f F_k^{previous}$$
(19)

$$\boldsymbol{\beta}_{k} = \boldsymbol{\beta}_{k}^{food} + \boldsymbol{\beta}_{k}^{best} \tag{20}$$

Where,  $V_f$  is the foraging speed,  $\omega_f$  is the foraging motion's inertia weight in the field [0, 1],  $F_k^{previous}$  is the final foraging movement,  $\beta_k^{food}$  is the food attractive and  $\beta_k^{best}$  is the preferable fitness's effect of each krill. Depending on the foraging speed's measured values, take as 0.02 ( $ms^{-1}$ ).

$$D_k = D^{\max} \delta \tag{21}$$

$$D_{k} = D^{\max} \left( 1 - \frac{I}{I_{\max}} \right) \delta$$
 (22)

Wherein,  $D^{\max}$  is the highest induction velocity,  $\delta$  is the random direction vector [0, 1].

Lastly, the location of each krill is updated to:

$$X_{k}^{next} = X_{k}^{current} + \Delta x_{k} \left( t \right)$$
(23)

$$\Delta x(t) = N_{k}(t) + F_{k}(t) + D_{k}(t)$$
(24)

Where, t is the krill's position.

### B. Cuckoo search

Through optimizing the conduct of some cuckoo species, CS is suggested that is swarm intelligence's a type technique for optimization problems. In CS, Lévy flights are consolidated that decides the cuckoo's walking steps. For simplicity in portraying CS, Yang and Deb adopted some of the idealized rules. For instance, every cuckoo is just relating to one egg; the preferable nests would be preserved and not be obliterated; the possible host nest number is unchangeable, and an egg is recognized through the host bird with a possibility. In CS, every egg in a nest shows a solution. The CS is to take use of the recently created better solutions in place of a moderately poor solution. In this research, we just looked at every nest that merely had an egg. Thus, in this research, the difference between the nest egg and solution was not identified. The CS technique can make a good harmony between a local arbitrary walk and the irregular global exploratory walk using a switching parameter. The former one can be represented as

$$X_{i}^{t+1} = X_{i}^{t} + \beta_{s} \otimes H\left(p_{a} - \varepsilon\right) \otimes \left(X_{j}^{t} - X_{k}^{t}\right)$$
(25)

Where  $X_{j}^{t}$  and  $X_{k}^{t}$  are two various solutions choice at random, H(u) is function of a Heaviside,  $\varepsilon$  is a number of random drawn from a regular distribution, and sis the step size. For the global random walk, it is combined with L évy flights as follows:

$$X_{i}^{t+1} = X_{i}^{t} + \beta L(s,\lambda), L(s,\lambda) = \frac{\lambda \Gamma(\lambda) \sin\left(\frac{\pi \lambda}{2}\right)}{\pi} \frac{1}{s^{1} + \lambda}, (s,s_{0} \succ 0)$$
(26)

Here,  $\beta \succ 0$  is the scaling factor of step size.

## C. Proposed Hybrid CS-KHA procedure

To ameliorate the fundamental's the search capacity KH technique; genetic techniques are added to the method [26]. Numerical outcomes when contrast with

5

Firstly in the proposed method, standard KHA uses

three movements to look for the best solutions and

engage these movements to lead the candidate solutions for the following generation. In this, KU operator is then

employed to carry out local search intensively to achieve

better solutions. This operator can since it abuses the

search space by Lévy flight. Towards the end of each

generation, the KA operator is employed to additionally

ameliorate the CS-KHA's the exploration by replacing the

worse krill's a fraction (pa) .Along these lines, this

component used in CS-KHA can completely extend the

strong the KHA's exploration and gain overcome the

absence of the KHA's weak exploitation . Above all, this

technique can additional unwind the inconsistency among exploration and exploitation effectively. Furthermore,

another basic change is the presentation of elitism scheme

into the CSKH. Likewise, with other population-based

methodologies, we employ a further focused elitism

technique to hold the preferable solutions for the

population. That elitism system forbids the preferable

krill from existence demolished through three movements

and KU/KA operator. By joining previously mentioned

KU/KA operator and concentrated elitism design into

unique KH technique to form a new CSKH algorithm

(see Algorithm 3).

other methods displays that KH II (only added crossover operator) performed the best.

In any case, KH can sometimes find it hard to come up with better solutions to several complicated problems. Consequently, in this article, a novel meta-heuristic technique by prompting KU operator and KA operator into KH to form a recent hybrid method, named CS-KHA is used to manage an OPF problem. The introduced KU/KA operators are roused by the authoritative CS algorithm. As such, in this paper, the property of cuckoo used in CS is supplemented to the krill to create excellent krill's a sort that can play out the KU/KA operator. The contrast amongst CSKH and KH is that the KU operator as a local search tool is used to adjust the new solution for every krill rather than rand walks used as KH's part (whereas in KH II, genetic generation techniques are employed). While KA operator is used to enhance further the exploration the method's ability by replacing some nests randomly thereby constructing new solutions. By the blending of CS and KH, CSKH can investigate the new search space with standard KH technique and KA operator and exploit the population information by KU operator. The main step of KU/KA operators used in CSKH method is presented by Algorithms 1 and 2, respectively.

Algorithm 1 KU operator	Algorithm 3 CSKH algorithm
Begin	Begin
Get a krill i and update its solution using Lévy flights	Step 1: Initialization. Set the t =1,the population
using Equation (25).	P, $V_f$ , $D^{\max}$ , and $N^{\max}$ , $p_a$ and <i>KEEP</i> .
Evaluate its quality $F_i$	Step 2: Fitness evaluation.
Select a krill j randomly.	Step 3: While t $\prec$ MaxGeneration do.
$lf(F_i \prec F_j)$	Sort the population.
Replace j with the novel solution and take the novel	Store the KEEP best krill.
solution as $X_{i+1}$	for $i = 1: N_p$ (all krill) do
Else	Perform the three motions.
Update the position of krill using equation (22) as $X_{i+1}$	Update the krill position by CU operator
end if	(see Algorithm 1).
End.	Evaluate each krill by $X_{i+1}$ .
Algorithm 2 KA operator 1. Begin 2. $K = rand (NP, D) \succ p_a$ . 3. $P_1 = P; P_2 = P$ 4. For $i = 1$ to NP (all krill) do. 5. $step = rand * (Y_i - Z_i);$	end for i Destroy the worse krill and build new ones by CA operator (see Algorithm 2). Replace the KEEP worst krill with the KEEP best krill. Sort the population. t = t + 1. Step 4: end while End.
6. $X_{new} = X_{i} + step \odot K(i,:);$	IV. OBJECTIVE FUNCTIONS AND STUDIED CASES
7. End for	A few contextual investigations with unique and multi-
8. For $i = 1$ to $NP$ (all krill) do.	objective have been made for networks IEEE 30-bus
9. If $F(X_{new}) \prec F(X_{i})$ then	IEEE 57-bus and IEEE 118-bus test systems. The

A few contextual investigations with unique and multiobjective have been made for networks IEEE 30-bus, IEEE 57-bus and IEEE 118-bus test systems. The essential characteristics of this networks exam system are given in [33].

A. IEEE 30 Bus system results

## Copyright © 2019 MECS

11. End if

12. End for 13.end

10.  $X_{new} = X_i; F(X_{new}) = F(X_i)$ 

#### A.1.Studied Cases

A total of 8 studies of cases were implementing in the first exam system (IEEE 30-bus exam system). The first two cases studies reduced OPF's single objective function. The rest is multi-objective optimization, which translates into a single target with a weighting factor, as in numerous past studies and recreated here. The definitions of the studied cases are expressed as follows:

#### Case 1: fuel cost's minimization

This is the fundamental OPF's objective function in all studies. The relationship among fuel cost (\$/h) and power generation Power (MW) is generally offered by two relationships, so the target function to be is reported as:

$$f(x,u) = \sum_{i=1}^{NG} a_i + b_i P_{G_i} + c_i P_{G_i}^2$$
(27)

Where  $a_i$ ,  $b_i$ ,  $c_i$  are the *i*-th generator's cost coefficients generating produce power. IEEE 30-bus system generators' cost coefficients can be seen in [39].

## *Case 2: fuel cost's minimization taking into account valve point effect*

The impact of the valve point should be taken into account for further practical and exact fuel cost function's modeling. The generating units with multi-valve steam turbines display a more prominent variety in the fuel-cost functions [32]. The valve loading multi-valve steam turbines' impact is modeled as function of sinusoidal, which's the absolute value is added to the fundamental cost function. The steam plant's actual cost curve function becomes non-continuous. The aim of reducing fuel cost of generating with valve-point effect is presented by [40]:

$$f(x,u) = \sum_{i=1}^{NG} \left( a_i + b_i P_{G_i} + c_i P_{G_i}^2 \right) + \left| d_i \times \sin\left( e_i \times \left( P_{G_i}^{\min} - P_{G_i} \right) \right) \right| (28)$$

Where,  $d_i$  and  $e_i$  are the coefficients that show the valve-point loading effect. The factors applied for calculations are given in [37].

## Case 3: Fuel cost's minimization and voltage stability enhancement

Voltage dependability issues are accepting developing consideration in power systems as network breakdown have been experienced in last because of instability of voltage. Under normal condition and in the wakw of being subjected to unsettling influence, the power system's steadiness is portrayed through its capacity to keep up whole bus voltages in suitable boundaries. A system goes into voltage instability's a condition when an unsettling influence, augmentation in load demand or variation in system term causes a dynamic and wild abatement in voltage[14]. Systems with long lines of transmission and overwhelming loading are further inclined to the problem of voltage instability. In power system, a system's enhancing voltage stability is a vital part. Each bus's *L*-index fills in as perfect power system stability's marker [42]. The index's value can be between 0 and 1, where 0 existence the no load case whereas 1 is the voltage collapse. If a power system has NL load (PQ) buses' number and NG generator (PV) buses' number , L-index Lj's value of bus *j* is can be explained as:

$$L_{j} = \left| 1 - \sum_{i=1}^{NG} F_{ji} \frac{V_{i}}{V_{j}} \right|, \text{ where } j = 1, 2, ..., NL \quad (29)$$

and

$$F_{ji} = - \left[ Y_{LL} \right]^{-1} \left[ Y_{LG} \right]$$

Where,  $Y_{LL}$  and  $Y_{LG}$  sub-matrices and are gotten from YBUS system matrix next separating load (PQ) buses and generator (PV) buses as shown in (29).

$$\begin{bmatrix} I_L \\ I_G \end{bmatrix} = \begin{bmatrix} Y_{LL} & Y_{LG} \\ Y_{GL} & Y_{GL} \end{bmatrix} \begin{bmatrix} V_L \\ V_G \end{bmatrix}$$
(30)

$$L_{\max} = \max\left(L_{j}\right) \quad j = 1, 2, \dots, NL \tag{31}$$

The indicator  $L_{\rm max}$  varies among 0 and 1 where the minimal the indicator, the further the system stable. Thus, enhancing voltage stability can be obtained by the reducing of  $L_{\rm max}$ . Hence, the objective function can be formulated as:

$$f(x,u) = \left(\sum_{i=1}^{NG} a_i + b_i P_{G_i} + c_i P_{G_i}^2\right) + \lambda_L \times L_{\max} \quad (32)$$

Where,  $L_{\text{max}}$  is chosen weight factor's value  $\lambda_{L}$  is 100.

## Case 4: Fuel cost's minimization and emission

Electrical power's generation from traditional energy's sources releases dangerous gases for the environment. The nitrogen oxides (NOx) and sulfur oxides (SOx)'s amount and emission in tones per hr (t/h) is higher with augmented in generated power (in p.u. MW) next the relationship presented in Eq. (33).

$$Emission = \sum_{i=1}^{NB} \left[ \left( \alpha_i + \beta_i P_{G_i} + \gamma_i P_{G_i}^2 \right) \times 0.001 + \omega_i e^{\left( \mu_i P_{G_i} \right)} \right]$$
(33)

Where,  $\alpha_i$ ,  $\beta_i$ ,  $\gamma_i$ ,  $\omega_i$  and  $\mu_i$  are all coefficients of emission provided in [41].

Therefore, the objective function of this case is given by:

$$f(x,u) = \left(\sum_{i=1}^{NG} a_i + b_i P_{G_i} + c_i P_{G_i}^2\right) + \lambda_E \times Emission \quad (34)$$

The weight factors are chosen as = 100 in this case.

Copyright © 2019 MECS

I.J. Image, Graphics and Signal Processing, 2019, 9, 1-17

#### Case 5: fuel cost's minimization and voltage deviation

Deviation of voltage is voltage quality's a measure in the network. The deviation's index is too vital from the security part. The indicator is expressed as cumulative voltages deviation of whole load buses in the network from nominal unity's value. Mathematically it is formulated as:

$$VD = \left(\sum_{p=1}^{NL} \left| V_{L_p} - 1 \right| \right) \tag{35}$$

The combining fuel cost's objective function and deviation of voltage is:

$$f\left(x,u\right) = \left(\sum_{i=1}^{NG} a_i + b_i P_{G_i} + c_i P_{G_i}^2\right) + \lambda_{VD} \times VD \quad (36)$$

Where, factor of weight is give a value of 100 as in [32,33].

## Case 6: Fuel cost minimization and active power loss

The power loss in system of transmission is certain because the lines have latent resistance. The active power loss to be reduced is formulated as:

$$P_{loss} = \sum_{i=1}^{nl} \sum_{j=1, j \neq i}^{nl} G_{ij} \left[ V_i^2 + V_j^2 - 2V_i V_j \cos(\delta_{ij}) \right]$$
(37)

A multi-objective case that aims at reducing fuel cost and active power loss simultaneously is transformed into single objective as:

$$f(x,u) = \sum_{i=1}^{NG} a_i + b_i P_{G_i} + c_i P_{G_i}^2 + \lambda_p \times P_{loss}$$
(38)

Where,  $P_{loss}$  is the active power loss and factor's value  $\lambda_n$  is selection as 40.

## Case 7: Fuel cost's minimization and voltage stability's enhancement

The objective function's formulation, comprising of both fuel cost taking into account the valve-point effect and voltage stability, this case's the objective function can be expressed as:

$$f(x,u) = \sum_{i=1}^{NG} (a_i + b_i P_i + c_i P_i^2) + d_i \times (e_i \times \sin(P_{gi}^{\min} - P_{gi})) + \lambda_L \times L_{\max}$$
(39)

The choice weight factor  $\lambda L$  is too 100.

Case 8: fuel cost's minimization, emission, voltage deviation and losses

Four objectives are put together for this case study. Fuel cost, emission, voltage deviation and active power loss in the network are whole reduced together. The objective function is presented by:

$$f(x,u) = \left(\sum_{i=1}^{NG} a_i + b_i P_i + c_i P_i^2\right) + \lambda_E \times$$
(40)  
Emission +  $\lambda_{VD} \times VD + \lambda_p \times P_{loss}$ 

The weight factors are choice as in [33] with  $\lambda_E = 19$ ,  $\lambda_{VD} = 21$  and  $\lambda_p = 22$  to balance between the objectives.

## V. RESULTS AND DISCUSSION

For optimizing's case 1 essential fuel cost, CS-KHA algorithms can produce to fuel costs of 799.0595 \$/h which satisfies all the system constraints, complying to the vital constraints of inequality on generator reactive power, load bus voltage and line capacity . Amongst whole the constraints of inequality, constraint on load bus voltage was discovered to be vital as the load buses' operating voltages are sometimes establish to be close the boundaries. Using the 3-methods (CS, KHA and CS-KHA), recent studies recorded better results when compared with present study are presented in table 2. The valve-point effect is studied for case 2 to achieve at a rise in cost than in case 1 with conclusive value of 830.0981\$/h, get by CS-KHA. In a nutshell, in spite of the variation in efficiency is seen between three methods, produce one or more technique's outcome used in our work are better than most of the results revealed in past literatures on the problem of OPF are presented in table 2.

Case 3 to case 8 are for OPF with multi-objective for 30-bus system. In these case studies, the joined objective function's fitness is the significant factor in ranking the different optimization techniques' outcome out. For a significant comparison, other techniques' fitness value is calculated and provided here employing the different objective functions' are weight factor. In multi-objective cases, an adjustment in weight factor e.g. elevated weight factor on fuel cost in case 3 the best values of both fuel cost and the system load buses' Lmax, CS-KHA gives preferable produce of 799.5625 and 0.1251 respectively, superior to the other comparable algorithms as appears in the table 2. Two objectives of cost and emission are concurrently reduced in case 4. Along with the fitness value, CS-KHA is at the cost and emission's least values in compared with in compared with other techniques presented in table 4.

Minimizing cost and voltage deviation (VD)'s in case 5, is achieved by CS-KHA which is the least among all other comparable techniques as appear in table 4.

In case 6 will reduce the cost and power loss. Table 3 shows' quick review that any these techniques' one or more CS, KHA and CS-KHA can give the preferable fitness values in whole the cases. Despite the fact that the preferable fitness is described by CS-KHA in case 6, a

transitional value fuel cost, the forming objectives' one, is accomplished. The active power loss's other goal is the

minimum when compared with other methods as appears in table 4.

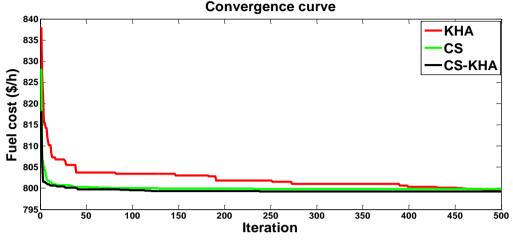


Fig.1. Convergent curves of Case 1

Table 1.7	The control	variables'	optimal	settings	for Cases	1-3.

Case1 Case2 Case3
Control variable CS-KHA KHA CS CS-KHA KHA CS CS-KHA KHA CS
P <sub>G1</sub> (MW) 177.7695 176.6985 177.0700 199.9957 199.9873 200.0000 178.3494 175.2915 178.5539
$P_{G2}$ (MW) 48.8746 48.4488 48.8674 43.0739 42.5401 43.8734 48.2403 47.5274 48.9785
P <sub>G5</sub> (MW) 21.0243 21.5532 21.3084 18.6343 19.1074 18.7891 20.5650 22.4648 21.3404
P <sub>G8</sub> (MW) 21.5808 22.6989 21.0859 10.0300 10.0177 10.0000 20.3673 22.6681 21.5868
P <sub>G11</sub> (MW) 10.8258 10.4866 11.8626 10.0000 10.0960 10.0000 12.7147 11.7468 10.0000
P <sub>G13</sub> (MW) 12.0000 12.1911 12.0000 12.0000 12.0241 12.0000 12.0000 12.3124 12.0000
$V_1(p.u)$ 1.1000 1.1000 1.1000 1.1000 1.1000 1.1000 1.1000 1.1000 1.1000
V <sub>2</sub> (p.u) 1.0894 1.0891 1.1000 1.0854 1.0866 1.1000 1.0892 1.0937 1.0829
$V_5(p.u)$ 1.0634 1.0631 1.0728 1.0588 1.0583 1.1000 1.0665 1.0674 1.0513
$V_8(p.u)$ 1.0696 1.0708 1.0796 1.0665 1.0657 1.0878 1.0742 1.0825 1.0544
$V_{11}(p.u)$ 1.1000 1.1000 1.0957 1.1000 1.0985 1.1000 1.0999 1.0999 1.1000
$V_{13}(p.u)$ 1.1000 1.0944 1.1000 1.0975 1.0867 1.0160 1.1000 1.0982 1.1000
$Qc_{10}(Mvar)$ 0.9873 0.7887 0 1.2012 0.3180 5.0000 4.8864 1.6654 5.0000
$Qc_{12}(Mvar)$ 4.2959 0.8533 0 1.9153 0.1754 5.0000 0.7211 2.2254 5.0000
$Qc_{15}(Mvar) = 3.0959 = 0.0015 = 5.0000 = 0.1687 = 0.0254 = 0 = 0.0187 = 0.9965 = 0$
$Qc_{17}(Mvar)$ 5.0000 3.0633 5.0000 0.0310 0.0426 5.0000 0.6251 2.9405 0
$Qc_{20}(Mvar)$ 4.4733 3.4508 3.5533 5.0000 3.3646 5.0000 0.0525 0.0173 0.8864
$Qc_{21}(Mvar)$ 4.4607 0.4024 5.0000 0.1385 2.6324 5.0000 0.8977 0.3830 5.0000
$Qc_{23}(Mvar)$ 0.3577 1.9594 5.0000 2.1640 0.8609 5.0000 2.4613 0.1354 0
$Q_{c_{24}}(Mvar)$ 5.0000 2.3827 5.0000 5.0000 1.2249 5.0000 4.0616 3.2836 5.0000
$Qc_{29}(Mvar)$ 3.4597 2.5427 5.0000 0.0572 2.9633 5.0000 0.3548 0.8722 5.0000
$T_{6-9}$ 1.0315 1.0077 0.9718 1.0763 1.0090 1.1000 0.9910 0.9888 0.9000
$T_{6-10}$ 0.9073 1.0210 1.1000 0.9027 1.0357 1.1000 0.9055 0.9503 1.1000
$T_{4-12} \qquad 0.9875  1.0364  1.1000  1.0359  1.0579  0.9000  0.9696  0.9850  1.1000$
$T_{28-27}$ 0.9785 0.9963 1.0194 0.9805 1.0057 1.1000 0.9417 0.9446 0.9358
Fuel cost (\$/h)         799.0595         799.4972         799.6547         830.0981         830.4199         833.5157         799.5625         799.8928         800.3034
VD 1.7638 1.1245 1.3088 1.2223 0.8337 0.9003 1.8465 1.7461 1.4380
Lmax 0.1290 0.1357 0.1350 0.1342 0.1393 0.1487 <b>0.1251 0.1253 0.1268</b>
Emission (ton/h) 0.3685 0.3653 0.3662 0.4425 0.4423 0.4424 0.3696 0.3608 0.3708
Ploss (MW) 8.6750 8.6771 8.7944 10.3339 10.3726 11.2625 8.8367 8.6110 9.0596

Table 2. the results obtained are compared for Cases 1-3

Case	e 1	Case	2	Case 3			
Algorithn	ns Fue	l cost (\$/h) Alg	orithms Fuel	cost (\$/h)	Algorithms	Fuel cost(\$/h)	Lmax
CS-KHA	799.0595	CS-KHA 8	30.0981	CS-KHA	799.5625	0.1251	
KHA	799.497	KHA 830.4	<b>4199</b> KH	A 799.	8928 0.125	3	
CS	799.6547	CS 833.51	.57 CS	800.303	34 0.1268		
BHBO[20	799.921	BSA [37]	830.7779	Gbest-AE	BC [16] 801.5	6821 0.1370	
ARCBBO	[12] 800.51	59 ICBO [32	2] 830.4531	MSA [	33] 801.2	248 0.13713	
BSA[37]	799.0760	CBO[32]	830.473	BSA[37]	800.3340	0.1259	
MSA[33]	800.5099	ECBO[32]	830. 587	ICBO [32	] 799.3277	0.1252	
BBO[37]	799.1267	DE[37]	830.4425	MDE [33]	802.0991	0.13744	

Case4 Case5 Case6 Control variable CS-KHA KHA CS CS-KHA KHA CS CS-KHA KHA CS
Control variable $C \in V \sqcup A = V \sqcup A = C \in V \sqcup A = V \sqcup A = C \in V \sqcup A = V \sqcup A = C \in V \sqcup A = V \sqcup A = C \in V \cup A = C \in V \cap A = C \in V \cup A = C \in C \cap A = C \in V \cup A = C \in C \cap A = C \in C \cap A = C \in C \cap A = C = C = C = C = C = C = C = C = C =$
P <sub>G1</sub> (MW) 112.7779 112.9464 111.7271 176.2886 176.2432 177.5324 105.5625 105.3719 102.2213
$P_{G2}$ (MW) 59.1035 58.7161 58.4399 49.1208 48.8217 49.1973 53.9578 52.9905 56.1303
P <sub>G5</sub> (MW) 28.0892 28.1822 27.3951 21.3698 21.6226 21.7154 36.9416 37.0963 37.2408
$P_{G8}(MW)$ 34.9991 35.0000 35.0000 22.0531 22.1836 22.8823 35.0000 34.9767 35.0000
P <sub>G11</sub> (MW) 26.5804 27.1184 30.0000 12.4129 12.3589 10 29.9505 29.6778 30.0000
P <sub>G13</sub> (MW) 26.9020 26.6188 26.2425 12 12 12 26.3434 27.7198 27.1722
$V_1(p.u)$ 1.1000 1.1000 1.000 1.0387 1.0462 1.0442 1.1000 1.1000 1.1000
V <sub>2</sub> (p.u) 1.0928 1.0924 1.1000 1.0215 1.0295 1.0278 1.0930 1.0922 1.1000
$V_5(p.u)$ 1.0696 1.0688 1.0806 1.0092 1.0145 1.0155 1.0736 1.0695 1.0833
$V_8(p.u)$ 1.0798 1.0800 1.1000 1.0044 1.009 1.0035 1.0824 1.0802 1.1000
$V_{11}(p.u)$ 1.0992 1.0996 0.9000 1.0797 1.0241 1.0397 1.0997 1.0961 1.1000
V <sub>13</sub> (p.u) 1.1000 1.0900 1.1000 0.9844 0.9835 0.9967 1.1000 1.1000 1.1000
Qc <sub>10</sub> Mvar) 1.1530 1.1760 5.0000 0 5 5 1.5790 3.5805 5.0000
$Qc_{12}(Mvar)$ 3.3798 2.9034 5.0000 5 2.1588 0 3.0622 0.0852 0
Qc <sub>15</sub> (Mvar) 5.0000 1.5069 5.0000 4.9985 5 0 0.1757 4.1400 0
$Qc_{17}(Mvar)$ 3.7785 0.2768 5.0000 0 0.0767 0 5.0000 2.2509 0
Qc <sub>20</sub> (Mvar) 4.1506 1.0711 5.0000 5 5 5 5.0000 2.5827 5.0000
Qc <sub>21</sub> (Mvar) 1.1979 0.7196 5.0000 5 5 5 5.0000 3.6976 5.0000
Qc <sub>23</sub> (Mvar) 0.0935 0.9665 5.0000 4.9587 0 5 2.9975 0.0588 4.2787
Qc <sub>24</sub> (Mvar) 5.0000 0.2050 5.0000 5 5 5 5.0000 0.0048 5.0000
$Q_{c_{29}}(Mvar)$ 1.4504 0.3080 5.0000 0 1.6478 5 2.2077 0.1971 2.1814
$T_{6-9}$ 1.0603 1.0374 1.0772 1.0888 1.0403 1.0596 1.0594 1.0402 1.1000
$T_{6-10}$ 0.9000 0.9597 0.9000 0.9 0.9 0.9 0.9 0.9023 0.9182 0.9000
$T_{4-12} \qquad 1.0186  1.0330  1.1000 \qquad 0.9451  0.9228  0.9303 \qquad 0.9945  1.0196  0.9966$
$T_{28-27} \qquad 0.9818  0.9857  1.1000 \qquad 0.9487  0.9613  0.9797 \qquad 0.9856  0.9767  0.9910$
Fuel cost (\$/h)         835.3821         835.9164         839.0130         803.6357         803.6580         803.7306         853.1469         854.6579         857.3526
VD 1.6529 1.1912 0.8867 0.1045 0.1117 0.1066 1.8266 1.5253 1.8731
Lmax 0.1300 0.1342 0.1487 0.1468 0.1480 0.1490 0.1288 0.1310 0.1276
Emission (ton/h) 0.2421 0.2422 0.2404 0.3637 0.3635 0.3677 0.2317 0.2311 0.2287
Ploss (MW) 5.0521 5.1820 5.4047 9.8452 9.8300 9.9274 <b>4.3558 4.4330 4.3646</b>

Table 3. the control variables' optimal settings for Cases 4-6.

Table 4. The results obtained are compared for Cases 4-6.

	Ca	se4	Case 5		Case	6			
Algorithms	Fuel cos	t (\$/h) Emi	ssion (t/h) Algo	orithms Fue	l cost (\$/h)	) VD (pu) A	lgorithms	Fuel cost(\$/h) Ploss	s(MW)
CS-KHA	835.3821	0.2421	CS-KHA 8	03.6357 0.	1045 C	S-KHA 853	.1469 4.3	3558	
KHA 83	35.9164	0.2422	KHA 803.6	580 0.1117	KHA	854.6579	4.4330		
CS 83	39.0130 (	0.2404	CS 803.73	06 0.1066	CS	857.3526	4.3646		
BSA [37]	835.0199	0.2425	BHBO [20]	804.5975	0.1262	FPA [33] 8	59.1915	4.5404	
GA-MPC[4]	1] 835.042	0.242	3 BSA [37]	803.4294	0.1147	MSA [33]	855.2706	4.7981	
MOGWO [1	9] 833.852	0.245	1 MSA[33]	803.3125	0.1084	MFO[33]	858.5812	4.5772	
NSGA-II[19	9] 859.849	0.3214	MFO[33]	803.7911	0.1056				
		FPA[33]	803.6638 0.	13659					

Table 5. The control variables' optimal settings for Cases 7 and 8.

	Case 7		Case 8
Control var	iable CS-KHA K	HA CS	S CS-KHA KHA CS
P <sub>G1</sub> (MW)	199.9573 200.0	408 200.000	001 122.7707 120.3378 121.4781
$P_{G2}(MW)$	44.0569 40.834	8 47.1590	0 52.2425 53.9179 51.5677
$P_{G5}(MW)$	17.8443 18.963	7 15.0000	0 31.2607 33.3589 30.5941
$P_{G8}$ (MW)	10.0000 11.208	8 10.0000	0 34.9961 35.0000 35.0000
P <sub>G11</sub> (MW)	10.0028 10.55	32 10.0000	00 26.4475 22.7272 30.0000
P <sub>G13</sub> (MW)	12.0214 12.00	00 12.0000	00 21.1133 23.4242 20.1360
$V_1(p.u)$	1.1000 1.1000	1.1000	1.0999 1.1000 1.1000
$V_2(p.u)$	1.0906 1.0880	1.1000	1.0890 1.0879 1.0887
V <sub>5</sub> (p.u)	1.0697 1.0665	1.0747	1.0627 1.0630 1.0636
V <sub>8</sub> (p.u)	1.0800 1.0752	1.0837	1.0718 1.0708 1.0733
V <sub>11</sub> (p.u)	1.0989 1.0995	1.1000	1.0560 1.0933 1.0206
V <sub>13</sub> (p.u)	1.1000 1.1000	1.1000	1.0325 1.0357 1.0562
Qc <sub>10(</sub> Mvar)	0 4.8665	5.0000	2.5177 0.9657 0
$Qc_{12}(Mvar)$	4.8593 0.119	0 0	0.1353 2.0934 0
$Qc_{15}(Mvar)$	3.5759 3.043	3 5.0000	0 4.8952 1.4256 0
Qc <sub>17</sub> (Mvar)	4.6437 2.887	8 0	3.2609 0.0210 5.0000
Qc <sub>20</sub> (Mvar)	2.5235 4.788	70	5.0000 3.0301 5.0000
Qc <sub>21</sub> (Mvar)	0.0014 4.725	3 0	0.1410 2.2403 5.0000
$Qc_{23}(Mvar)$	4.2770 4.018	1 5.0000	4.7800 0.0133 0
Qc <sub>24</sub> (Mvar)	0.2174 2.130	4 5.0000	0 0.0437 0.4552 0
Qc <sub>29</sub> (Mvar)	0.6333 2.986	90	0.5568 0.8862 5.0000
T <sub>6-9</sub>	0.9844 1.0277	1.1000	1.0996 1.0405 1.1000

T <sub>6-10</sub>	0.9000	0.9057	0.9000	0.9766	1.0636	0.9523	
T <sub>4-12</sub>	0.9658	0.9706	0.9919	1.0791	1.0482	1.1000	
T <sub>28-27</sub>	0.9469	0.9567	0.9472	1.0144	1.0126	1.0328	
Fuel cost (2	\$/h) 830.5	5273 830	0.3209 831.	7243	828.8532	832.1724	831.1796
VD	1.9815	1.9553	1.7393	0.4827	0.5205	0.5015	
Lmax	0.1248	0.1253	0.1253	0.1446	5 0.1440	0.1450	
Emission (	(ton/h) 0.44	426 0.4	422 0.443	7 0	0.2537 0.2	2508 0.2	2517
Ploss (MW	/) 10.48	28 10.20	013 10.759	1 5.	4308 5.3	660 5.3°	759

Table 6. The results obtained are compared for Cases 7 and 8.

Case 7	Case 8
Algorithms Fuel cost(\$/h)	Lmax Algorithms Fuel cost(\$/h) Ploss (MW) VD(p.u) Emission (ton/h)
CS-KHA 830.5273 0.1248	CS-KHA 828.8532 5.4308 0.4827 0.2537
KHA 830.3209 0.1253	KHA 832.1724 5.3660 0.5205 0.2508
CS 831.7243 0.1253	CS 831.1796 5.3759 0.5015 0.2517
BSA [37] 832.7029 0.126	
MSA	[33] 830.639 5.6219 0.29385 0.25258
MFC	[33] 830.9135 5.5971 0.33164 0.2523
MDE	[33] 829.0942 6.0569 0.30347 0.2575

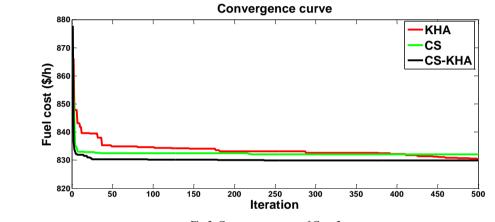


Fig.2. Convergent curves of Case 2

Important amelioration in fuel cost seen (through CS-KHA) in case 7's for multi-objective optimization where both cost considering the valve-point effect and *L*-max are minimized. Preferable to the other comparable algorithms as appears in table 6.

Cost, real power loss, emission and voltage deviation concurrently reduced four objectives are in case 8. Along with the fitness value, CS-KHA is at the cost and loss's least values in contrast with MSA [33] and FPA [33], as shown in Table 6. Graphical comparison the convergence of three proposed techniques for Case 1 and Case 2 of the objective functions related to the fuel cost is shown in Figures 1 and 2 respectively. The convergence speeds are Not distinctly various between the techniques. Be that as it may, fast and surprising convergence is seen for both KHA and CS-KHA during the search process's first phase. KHA converges to the ideal solution more consistently. Two-objective cases' convergences are given in Fig.3. (3.a and 3.b), Fig. 4. and Fig. 5. (5.a and 5.b). For clarity, only one technique's convergence achieving optimal fitness value is shown in the graph.

### Comparison among CS, KHA and CS- KHA

Table 7. Shows the statistical summary of 30 runs using three proposed algorithm as the fundamental search technique for each study carried out. The columns denote the best, worst, average and standard deviation values of the objective function in every case. It is clear that no single technique is capable to issue the best mean values in whole the cases. CS-KHA is found to be superior to KHA and CS in all cases for 30-bus and 57-bus system.

## A. Results of IEEE 57-bus test system

So as to exam the usability of the suggested CS-KHA technique, a greater test system is take into account in this article, which is the IEEE 57-bus test system. 57-bus system's general system data are given in [43].

## CASE 9: fuel cost minimization

The goal of this case is to reduce the total generating fuel cost. Hence, this case's the objective function is presented by (27). The CS-KHA is implementation so as to get the optimal settings for this case and the gained results are presented in Table 8. In this case minimizing the fuel cost's fundamental objective produce to a value of 41660.2273 \$/h by CS-KHA, the most minimal when compared with other recent studies' substantial results as seen in Table 9.

### CASE 10: Fuel cost minimization and voltage deviation

The purpose of the objective function is to reduce simultaneously both fuel cost and voltage deviation. The transformed single objective function next equation (36) with weight factor  $\lambda_{VD}$  is chosen as 100. The results of such optimization using the suggested CS-KHA technique are given in Table 8. This table shows that the VD has been decrease from (1.5991 p.u.) to (0.6940 p.u.) compared with CASE 9. Hence, the cost has slightly augmented from (41660.2273 \$/h) to (41712 \$/h) compared with CASE 9.

## B. Results of IEEE 118-bus test system:

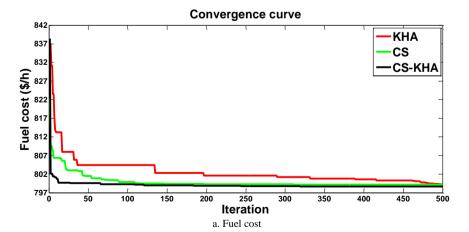
## CASE 11: Fuel cost minimization

To prove performance of the suggested hybrid CS-KHA, the large-scale IEEE 118-bus system is deliberated for study goal, the essential characteristics are presented in [43]. In general, the efficiency of the proposed algorithm is excellent for variables' higher number in constrained optimization problems. Therefore, CS-KHA method is utilized to the system to decrease fuel cost. Hence, this case's objective function is presented by (27). The CS-KHA is implemented so as to get the optimal settings for this case and the gained results are presented in Table10. In this case, minimizing the fuel cost's fundamental objective produce to a value of 135260.45\$/h by CS-KHA, the most minimal when compared with other recent studies' substantial results as seen in Table 11.

## VI. CONCLUSION

In present study, a new Meta hybrid heuristic CSKH technique has been suggested to solve the problem of OPF. By merging the merits KU/KA operator of CS technique with the KH technique. Hence, the KH is improved and the CSKH algorithm is evaluated numerically.

The detailed expression of a new variant of KH algorithm is given, and the KU operator is adjusted dynamically in KU process. In the proposed hybrid CSKHA, a greedy option was used, often surpassing the standard CS and KH. Moreover, so as to more ameliorate the CSKH's exploration, each generation of end KA operators will be a small number of poor krill thrown away, and replaced by new randomly generated krill. The problem of OPF has been expressed as a constrained optimization problem where many objective functions have been taking into account to decrease the fuel cost, to enhance the voltage stability and to improve the voltage profile. However, non-smooth piece-wise quadratic cost objective function has been deliberated. The feasibility of the suggested CS-KHA technique for solving problems of OPF is confirm by apply three standard test power systems. The results of the simulation prove the success and robustness of the suggested method to solve problem of OPF in small and large test systems. In addition, the suggested methods in this study achieve significantly better than several other equivalent optimization techniques in obtaining solutions of OPF. Decrease in hourly operation cost has been based almost in whole the cases studied in the context of this literature. In order to add more complex objectives function when solving OPF problems, no method is the best way to solve all OPF problems. Therefore, there is always a require for a new method, capable of successfully solving as many OPF problems as possible. However, increased capability is often achieved by hybridizing method and deterministic optimization techniques. In the future, different settings of optimization techniques used in this article are chosen by trial and error to improve convergence characteristics and these settings can be optimized for improved effectiveness. Various types of sources energy, like solar cells, wind turbines can be involved in solving OPF problems.



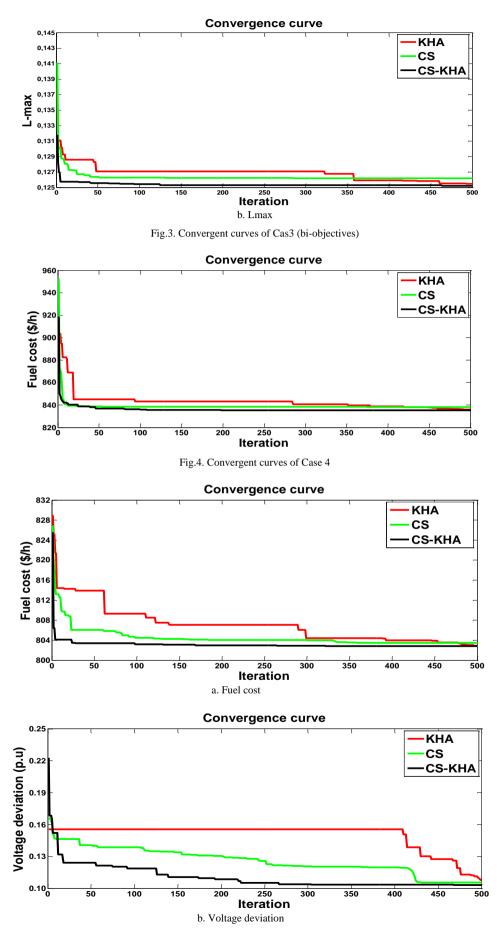


Fig.5. Convergent curves of the objectives of Case 5

Table 7. Summary of statistical indices	of the CS-KHA	with CS. KH	A for Cases 1-10
ruble 7. Builling of studistical marces	or the co min	$\cdots$	

				(	CS-KHA			KHA	4		CS		
	Case.no	Best	Worst	Mean	Std dev	Best	Worst	Mean	Std d	ev Best	Worst	Mean	Std dev
Cace1	799.0595	799.4923	799.17	51 0.002	3 799.49'	72 799.9	9512	799.7572	0.024	799.6547	800.1054	799.95	13 .0321
Case2	830.0981	830.6713	830.162	25 0.019	830.419	9 830.9	922 8	30.6918	0.033	833.5157	833.9145	833.73	327 0.029
Case3	799.5625	799.8921	799.700	0.03	799.8928	800.41	800	0.1367 0.	.043 8	300.3034	800.9133	800.6723	0.0352
Case4	835.3821	835.8811	835.592	20 0.001	5 835.916	4 836.5	764 8	36.2321	0.0191	839.013	0 839.770	0 839.32	205 0.027
Case5	803.6357	803.980	803.810	0 0.023	803.6580	804.210	04 803	3.9683 0	.03202	803.7306	804.2710	803.936	0 0.0331
Case6	853.1469	853.5361	853.274	42 0.002	6 854.657	79 855.3	8519	854.9914	0.041	857.352	857.972	20 857.6	5437 0.03602
Case7	830.5273	830.9407	830.720	0.003	1 830.320	09 830.9	9859	830.7303	0.034	2 831.72	43 832.192	26 831.	9751 0.0284
Case8	828.8532	829.2302	828.97	0.038	832.172	4 832.8	743	832.5126	0.037	5 831.179	6 831.699	01 831.4	425 0.0223
Case9	41660.227	73 41660.8	40 4166	0.5703 0	.04 41673	3.5922 4	1674.1	10 4167	3.9078	0.051 41	717.8801 4	1718.471	3 41718.0721 0.0
Case10	) 41712 4	1712.770	1 41712.3	3923 0.06	2 41705	41705.	6203 4	41705.27	4 0.042	1 41791	41791.89	12 41791	. 4822 .037

		Case 9	1		Case 10	
Control variat	ole CS-KHA		CS	CS-KHA	KHA	CS
$P_{G1}(MW)$	143.4297	145.0358	140.9221	140.6795	141.9955	5 146.915
$P_{G2}$ (MW)	87.0645	98.1294	77.7157	94.9802	92.1514	100.0000
$P_{G3}(MW)$	45.1917	47.2053	40.0000	47.1461	45.7668	40.0000
P <sub>G6</sub> (MW)	67.0035	54.0795	100.0000	66.5315	78.1945	100.0000
P <sub>G8</sub> (MW)	459.5789	472.6903	453.4311	460.6278	460.5117	478.9845
$P_{G9}(MW)$	99.7951	81.2897	100.0000	94.4812	89.2280	30.0000
P <sub>G12</sub> (MW)	363.2292	367.0996	354.6953	362.1398	358.8398	371.700
$V_1(p.u)$	1.0713	1.0695	1.0552	1.0206	1.0198	1.1000
$V_2(p.u)$	1.0746	1.0734	1.0577	1.0244	1.0253	1.1000
$V_3(p.u)$	1.0603	1.0611	1.0461	1.0119	1.0155	1.1000
$V_6(p.u)$	1.0597	1.0594	1.0654	1.0150	1.0264	1.1000
$V_8(p.u)$	1.0755	1.0778	1.1000	1.0384	1.0503	1.1000
V <sub>9</sub> (p.u)	1.0710	1.0699	1.0739	1.0240	1.0329	1.1000
$V_{12}(p.u)$	1.0582	1.0562	1.0453	1.0040	1.0070	1.1000
Qc <sub>18(</sub> Mvar)	6.8293	4.8640	20.0000	10.8442 8	3.0117	0
Qc <sub>25</sub> (Mvar)	14.0936	16.3750	9.1658	6.4490	15.9809	15.1607
Qc <sub>53</sub> (Mvar)	11.2626	17.1950	20.0000	13.4479	11.0521	20.0000
T <sub>4-18</sub>	1.0432	0.9608	0.9000	0.9583	1.0192	0.9000
T <sub>4-18</sub>	0.9543	1.0416	1.1000	1.0017	0.9868	1.1000
$T_{21-20}$	0.9981	1.0422	1.1000	0.9981	0.9773	1.1000
T <sub>24-25</sub>	1.0345	1.0436	1.1000	0.9680	0.9543	0.9000
T <sub>24-25</sub>	1.0039	1.0439	0.9000	0.9574	1.0740	1.1000
T <sub>24-26</sub>	1.0175	1.0326	1.0668	1.0298	1.0136	1.0171
T <sub>7-29</sub>	0.9975	1.0014	1.0565	0.9801	0.9951	1.0648
T <sub>34-32</sub>	0.9533	0.9558	0.9000	0.9283	0.9354	0.9388
$T_{11-41}$	0.9016	0.9495	0.9000	0.9000	0.9001	0.9000
T <sub>15-45</sub>	0.9869	0.9883	0.9795	0.9509	0.9513	1.0178
T <sub>14-46</sub>	0.9832	0.9756	0.9796	0.9527	0.9606	1.1000
T <sub>10-51</sub>	0.9948	0.9876	0.9951	0.9725	0.9861	1.0697
T <sub>13-49</sub>	0.9579	0.9450	0.9000	0.9170	0.9177	0.9738
T <sub>11-43</sub>	1.0219	0.9863	1.1000	0.9418	0.9782	1.1000
$T_{40-56}$	0.9860	0.9959	1.1000	1.0432	0.9771	0.9000
T <sub>39-57</sub>	0.9993	0.9698	0.9869	0.9218	0.9373	1.1000
T <sub>9-55</sub>	1.0120	1.0285	1.1000	1.0029	1.0128	1.1000
Fuel cost (\$/h)	41660.227	3 41673.5	5922 41717	.8801 417	712 4170	)5 41791
VD	1.5991	1.6959	1.7060	0.6940	0.7004	1.5878
Lmax	0.2816	0.2800	0.2775	0.2931	0.2935	0.2870
Emission (to	on/h) 1.356	5 1.411		1.3554		1.4690
Ploss (MW)	14.4929	14.7297		15,7861	15.8877	16.8061

Table 9. The results obtained are compared for Cases 9 and 10.

Case 9			Case 10		
Algorithms	Fuel cost(\$/h)	Algorithms	Fuel cost	(\$/h) VD (p.u)	
CS-KHA	41660.2273	CS-KHA	41712	0.6940	
KHA	41673.5922	KHA	41705	0.7004	
CS	41717.8801	cs 4	1791	1.5878	
MSA [33]	41673.7231	MSA [33]	41714.98	51 0.67818	
ICBO [32]	41697.3324	FPA [33]	41726.37	58 0.69723	

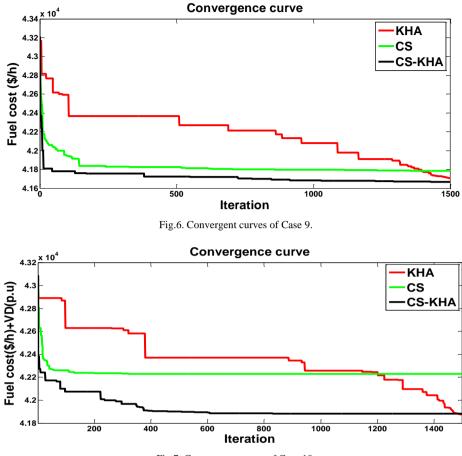


Fig.7. Convergent curves of	of Case 10.
-----------------------------	-------------

Table 10. The control variables	optimal settings for case11.
---------------------------------	------------------------------

$\begin{array}{c c c c c c c c c c c c c c c c c c c $	00
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	CS
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	33
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	14
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	76
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	67
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	92
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	66
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	37
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	60
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	48
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	17
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	74
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	76
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	52
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	18
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	30
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	25
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	30
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	35
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	91
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	33
$P_{G61}(MW) = 128.9333 = 126.3616 = 116.7174 = V_{G61}(p.u) = 1.0857 = 1.0959 = 1.0959$	19
	39
	19
$P_{G65}$ (MW) 30.0414 30.6740 33.8130 $V_{G65}$ (p.u) 1.0886 1.0891 1.05	24
P <sub>G66</sub> (MW) 274.4206 296.6764 274.6836 V <sub>G66</sub> (p.u) 1.0981 1.1000 1.09	
$P_{G69}$ (MW) 290.2244 273.8381 285.3788 $V_{G69}$ (p.u) 1.0819 1.0947 1.09	21
$\frac{P_{G70} (MW)}{P_{G70} (Pu)} = \frac{10000}{33.8793} = \frac{10000}{31.0321} = \frac{10000}{30.0310} = \frac{10000}{V_{G70} (Pu)} = \frac{10000}{1.0760} = \frac{10000}{1.0680} = \frac{10000}{1.0760} = \frac{10000}{1.0680} = \frac{10000}{1.0760} = \frac{10000}$	

$\begin{array}{c c c c c c c c c c c c c c c c c c c $				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G72</sub> (MW)	30.0000		V <sub>G72</sub> (p.u) 1.0847 1.0782 1.0618
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G76</sub> (MW)	31.1843	30.0000 30.0515	V <sub>G76</sub> (p.u) 1.0481 1.0534 1.0537
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G80</sub> (MW)	353.3451	328.0506 339.0098	V <sub>G80</sub> (p.u) 1.0578 1.0871 1.0748
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G85</sub> (MW)	30.4117	34.3764 30.0251	V <sub>G85</sub> (p.u) 1.0698 1.0849 1.0867
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G87</sub> (MW)	31.2043	31.2010 31.2000	V <sub>G87</sub> (p.u) 1.0883 1.0856 1.0802
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G89</sub> (MW)	373.0515	5 343.3753 383.0308	V <sub>G89</sub> (p.u) 1.0766 1.1000 1.0966
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G90</sub> (MW)	30.0217	30.0053 30.0816	V <sub>G90</sub> (p.u) 1.0543 1.0908 1.0790
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G91</sub> (MW)	30.1360	31.2499 33.4771	V <sub>G91</sub> (p.u) 1.0621 1.0926 1.0810
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		30.0000	31.6228 30.0239	V <sub>G92</sub> (p.u) 1.0568 1.0932 1.0839
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G99</sub> (MW)	31.5839	30.1290 32.1729	V <sub>G99</sub> (p.u) 1.0515 1.0699 1.0605
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G100</sub> (MW)	161.0120	5 174.5208 163.4482	V <sub>G100</sub> (p.u) 1.0395 1.0786 1.0654
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G103</sub> (MW)	42.2950	42.1514 42.2731	V <sub>G103</sub> (p.u) 1.0212 1.0726 1.0593
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G104</sub> (MW)	30.8340	31.1019 30.1950	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G105</sub> (MW)	30.1658	30.0082 30.0294	V <sub>G105</sub> (p.u) 1.0123 1.0751 1.0472
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G107</sub> (MW)	30.7389	30.1938 30.7178	V <sub>G107</sub> (p.u) 0.9973 1.0717 1.0433
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G110</sub> (MW)	32.0056	30.6153 30.4068	V <sub>G110</sub> (p.u) 0.9894 1.0791 1.0417
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		40.8006	40.8581 40.8015	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G112</sub> (MW)	30.6941	30.1776 35.3112	V <sub>G112</sub> (p.u) 0.9775 1.0721 1.0298
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G113</sub> (MW)	30.5556	30.1612 43.2123	V <sub>G113</sub> (p.u) 1.0584 1.0584 1.0260
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	P <sub>G116</sub> (MW)	31.5470	30.1511 30.6720	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$Qc_5(Mvar)$	1.0968	0.1341 0.4603	T <sub>(8-5)</sub> 1.0269 1.0527 1.0180
$\begin{array}{c ccccc} \hline Qc_{44}(Mvar) & 10.4951 & 0.3568 & 0.0083 & T_{(38-37)} & 0.9561 & 0.9903 & 0.9672 \\ \hline Qc_{45}(Mvar) & 0.0001 & 2.6926 & 1.0940 & T_{(63-59)} & 0.9402 & 0.9071 & 0.9072 \\ \hline Qc_{46}(Mvar) & 6.3599 & 0.6672 & 17.7909 & T_{(64-61)} & 1.0339 & 0.9722 & 0.9434 \\ \hline Qc_{48}(Mvar) & 0.3103 & 0.6422 & 0.3959 & T_{(65-66)} & 1.0317 & 1.0952 & 1.0250 \\ \hline Qc_{74}(Mvar) & 0.5937 & 0.0949 & 12.9769 & T_{(68-69)} & 1.0046 & 1.0947 & 0.9504 \\ \hline Qc_{79}(Mvar) & 0.4359 & 1.0046 & 1.7815 & T_{(81-80)} & 1.0284 & 0.9213 & 0.9667 \\ \hline Qc_{83}(Mvar) & 2.7523 & 0 & 2.0127 & Objective functions \\ \hline Qc_{105}(Mvar) & 1.1846 & 2.5892 & 10.9604 & Fuel cost (\$/h) & 135260.45 & 135400.78 & 135610.321 \\ \hline Qc_{107}(Mvar) & 4.1717 & 0.0284 & 4.9321 & Ploss (MW) & 56.4548 & 58.1287 & 53.3527 \\ \hline \end{array}$	Qc <sub>34</sub> (Mvar)	0.0395	0.0656 7.8806	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>37</sub> (Mvar)	1.7660	7.3596 2.7258	Т <sub>(30-17)</sub> 0.9923 1.0165 1.0267
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>44</sub> (Mvar)	10.4951	0.3568 0.0083	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>45</sub> (Mvar)	0.0001	2.6926 1.0940	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>46</sub> (Mvar)	6.3599	0.6672 17.7909	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>48</sub> (Mvar)	0.3103	0.6422 0.3959	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>74</sub> (Mvar)	0.5937	0.0949 12.9769	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>79</sub> (Mvar)	0.4359	1.0046 1.7815	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Qc <sub>82</sub> (Mvar)	2.6580	0 2.5440	
Qc <sub>105</sub> (Mvar)         1.1846         2.5892         10.9604         Fuel cost (\$/h)         135260.45         135400.78         135610.321           Qc <sub>107</sub> (Mvar)         4.1717         0.0284         4.9321         Ploss (MW)         56.4548         58.1287         53.3527	Qc <sub>83</sub> (Mvar)	2.7523		Objective functions
Qc107(Mvar)         4.1717         0.0284         4.9321         Ploss (MW)         56.4548         58.1287         53.3527	Qc <sub>105</sub> (Mvar)	1.1846	2.5892 10.9604	Fuel cost (\$/h) 135260.45 135400.78 135610.321
$Q_{c_{110}}(Mvar)$ 4.0167 0.57250.0614	Qc <sub>107</sub> (Mvar)	4.1717	0.0284 4.9321	
	$Qc_{110}(Mvar)$	4.0167	0.57250.0614	

Table 11. Th	he results	obtained	are o	compared	for	Case	11.
--------------	------------	----------	-------	----------	-----	------	-----

Case	Algorithms	Fuel cost (\$/h)	
	CS-KHA	135260.45	
Case 11	KHA	135400.78	
	CS	135610.321	
	BSA [37]	135333.4743	
	ABC [37]	135304.3584	
	BBO [37]	135263.7289	

#### REFERENCES

- Shaheen, A.M., El-Sehiemy, R.A., Farrag, S.M., "Solving multi-objective optimal power flow problem via forced initialised differential evolution algorithm," IET Generation, Transmission and Distribution 2016, 10(7), pp. 1634-1647
- [2] Huneault M, Galiana FD. A survey of the optimal power flow literature. IEEE Trans Power Syst 1991; 6(2):762–70.
- [3] Chowdhury B, Rahman S. A review of recent advances in economic dispatch. IEEE Trans Power Syst 1990; 5 (4): 1248–59.
- [4] T. Niknam, M. Rasoul Narimani, M. Jabbari, A.R. Malekpour, A modified shuffle frog leaping algorithm for multi-objective optimal power flow, Energy 36 (2011) 6420–6432,
- [5] Roa-Sepulveda C, Pavez-Lazo B. A solution to the optimal power flow using simulated annealing. Int J Electri Power Energy Syst 2003; 25:47–57.
- [6] L.L. Lai & J.T. Ma. Improved genetic algorithms for optimal power flow under both normal and contingent

operation states. Electrical Power and Energy Systems, 19, 287-292, 1997.

- [7] S.R. Paranjothi, K. Anburaja, Optimal power flow using refined genetic algorithm, Electr. Power Components Syst. 30 (2002) 1055–1063.
- [8] Shaheen, A.M., Farrag, S.M., El-Sehiemy, R.A., "MOPF solution methodology,", IET Generation, Transmission and Distribution 2017 11(2), pp. 570-581
- [9] M. Abido, Optimal power flow using Tabu search algorithm, Electric Power Syst. Res. 30 (2002) 469–483.
- [10] Ghasemi M, Ghavidel S, Ghanbarian MM, Massrur HR, Gharibzadeh M. Application of imperialist competitive algorithm with its modified techniques for multi-objective optimal power flow problem: a comparative study. Inf Sci (Ny) 2014; 281:225–47.
- [11] M. A. Abido, Optimal power flow using particle swarm optimization, Electrical Power and Energy Systems, 24, 563-571, 2002.
- [12] A. Ramesh Kumar & L. Premalatha, Optimal power flow for a deregulated power system using adaptive real coded biogeography-based optimization, Electrical Power and Energy Systems, 73,393–399, 2015.

- [13] P.K. Roy, S.P. Ghoshal, S.S. Thakur, Biogeography based optimization for multi-constraint optimal power flow with emission and non-smooth cost function, Expert Syst. Appl. 37 (2010) 8221–8228.
- [14] Bhattacharya, A., & Chattopadhyay, P. K. (2011). Application of biogeography-based optimization to solve different optimal power flow problems. IET generation, transmission & distribution, 5(1), 70-80.
- [15] El-Sehiemy, R.A., Shafiq, M.B., Azmy, A.M., "Multiphase search optimization algorithm for constrained optimal power flow problem," International Journal of Bio-Inspired Computation, 2014, 6(4), pp. 275-289.
- [16] R. Roy & H.T. Jadhav, Optimal power flow solution of power system incorporating stochastic wind power using Gbest guided artificial bee colony algorithm, Electrical Power and Energy Systems, 64, 562–578, 2015.
- [17] A.R. Bhowmik, A.K. Chakraborty, Solution of optimal power flow using non dominated sorting multi objective opposition based gravitational search algorithm, Int. J. Electr. Power Energy Syst. 64 (2015) 1237–1250.
- [18] K. Ayan, U. Kılıc, B. Baraklı, Chaotic artificial bee colony algorithm based solution of security and transient stability constrained optimal power flow, Int. J. Electr. Power Energy Syst. 64 (2015) 136–147.
- [19] L. Dilip, R. Bhesdadiya, P. Jangir, Optimal Power Flow Problem Solution Using Multi-objective Grey Wolf Optimizer Algorithm, Springer Nature Singapore, Pte. Ltd. 2018.
- [20] Bouchekara HREH. Optimal power flow using blackhole-based optimization approach. Appl Soft Comput J 2014; 24:879–88.
- [21] Bouchekara HREH, Abido Ma, Boucherma M. Optimal power flow using teaching-learning-based optimization technique. Electr Power Syst Res 2014; 114:49–59.
- [22] Attia, A.-F., El Sehiemy, R.A., Hasanien, H.M., "Optimal power flow solution in power systems using a novel Sine-Cosine algorithm," International Journal of Electrical Power and Energy Systems, 2018, 99, pp. 331-343
- [23] Daryani N, Hagh MT, Teimourzadeh S. Adaptive group search optimization algorithm for multi-objective optimal power flow problem. Appl Soft Comput 2016; 38:1012– 24.
- [24] A. Khelifi, S. Chettih, B. Bentouati, A new hybrid algorithm of particle swarm optimizer with grey wolves' optimizer for solving optimal power flow problem, Leonardo Electronic J. of P. & Technologies. 2018, 249-270.
- [25] M. AlRashidi, M. El-Hawary, Applications of computational intelligence techniques for solving the revived optimal power flow problem, Electr. Power Syst. Res. 79 (2009) 694–702.
- [26] A.H. Gandomi, A.H. Alavi, Krill herd: a new bio-inspired optimization algorithm, Commun. Nonlinear Sci. Numer. Simulat. 17 (2012) 4831–4845.
- [27] Wang G-G, Guo L, Gandomi AH, Hao G-S, Wang H, Chaotic krill herd algorithm. Inf Sci 274 (2014) 17-34.
- [28] Bentouati, B., Chettih, S., El-Sehiemy, R., "A chaotic firefly algorithm framework for non-convex economic dispatch problem," Electrotehnica, Electronica, Automatica (EEA), 2018, 66(1), pp. 172-179
- [29] Xin-She Yang, Flower Pollination Algorithm for Global Optimization. In: Unconventional Computation and Natural Computation, Vol. 7445, Springer Lecture Notes in Computer Science, Berlin, Heidelberg, 2012, pp. 240– 249.
- [30] Ghasemia M, Taghizadeh M, Ghavidel S, Abbasian A. Colonial competitive differential evolution: an

experimental study for optimal economic load dispatch. Appl Soft Comput 2016; 40:342e63.

- [31] B. Mandal, P. Kumar Roy, Multi-objective optimal power flow using quasi-oppositional teaching–learning-based optimization, Appl. Soft Comput. 21(2014) 590–606.
- [32] Bouchekara, H. R. E. H., Chaib, A. E., Abido, M. A., & El-Sehiemy, R. A. (2016). Optimal power flow using an Improved Colliding Bodies Optimization algorithm. Applied Soft Computing, 42, 119-131.
- [33] Mohamed, A. A. A., Mohamed, Y. S., El-Gaafary, A. A., & Hemeida, A. M. (2017). Optimal power flow using moth swarm algorithm. Electric Power Systems Research, 142, 190-206.
- [34] Bachir Bentouati et al, Optimal Power Flow using the Moth Flam Optimizer: A case study of the Algerian power system, TELKOMINIKA, 1, pp. 3. 2016.
- [35] Bentouati, B., Chettih, S., El Sehiemy, R., Wang, G.-G., "Elephant herding optimization for solving non-convex optimal power flow problem," Journal of Electrical and Electronics Engineering, 201710(1), pp. 31-36
- [36] Bentouati, B., Chettih, S., Djekidel, R., El-Sehiemy, R.A.,
   "An efficient chaotic cuckoo search framework for solving non-convex optimal power flow problem," International Journal of Engineering Research in Africa, 2017, 33, pp. 84-99
- [37] Chaib, A. E., Bouchekara, H. R. E. H., Mehasni, R., & Abido, M. A. (2016). Optimal power flow with emission and non - smooth cost functions using backtracking search optimization algorithm. International Journal of Electrical Power & Energy Systems, 81, 64-77.
- [38] Wang G, Gandomi AH, Alavi AH. An effective krill herd algorithm with migration operator in biogeography-based optimization. Appl Math Model 2014; 38(9-10):2454–62.
- [39] El-Hosseini, M.A., El-Sehiemy, R.A., Haikal, A.Y., "Multi-objective optimization algorithm for secure economical/emission dispatch problems," Journal of Engineering and Applied Science, 2014 61(1), pp. 83-103
- [40] Biswas, P. P., Suganthan, P. N., & Amaratunga, G. A. (2017). Optimal power flow solutions incorporating stochastic wind and solar power. Energy Conversion and Management, 148, 1194-1207.
- [41] H. R. E. H. Bouchekara, Chaib, A. E., & Abido, M. A. Optimal power flow using GA with a new multi-parent crossover considering: prohibited zones, valve-point effect, multi-fuels and emission. Electr Eng (2016).
- [42] Kessel, P., & Glavitsch, H. (1986). Estimating the voltage stability of a power system. IEEE Transactions on Power Delivery, 1(3), 346-354.
- [43] R.D. Zimmerman, C.E. Murillo-Sánchez, R.J. Thomas, Matpower (Available at :) http:// www. pserc. cornell. edu/ matpower.

## **Authors' Profiles**



Aboubakr Khelifi was born in Laghouat (Algeria). He received master degrees in Electrical Engineering in 2015 from Amar Telidji Laghouat, University. He is currently a PhD student at the same University. His research interests are focused on the electrical power system, optimal power flow, and optimization techniques.

E-mail address: a.khelifi@lagh-univ.dz



**Bentouati Bachir** was born in Laghouat, Algeria, on August 22, 1990. He received license, master and doctor degrees in Electrotechnic and Electrical Power System in 2010, 2012 and 2018 respectively from Laghouat university. His areas of research include optimal power flow, Artificial intelligence and

optimization techniques.



**Chettih Saliha** was born on 11 may 1971 in Laghouat/Algeria. She earned his PhD degree in Electro-technology from the University of Amar Telidji. She joined the faculty of the Technology He joined the faculty of the Technology at the University of Amar Telidji, Laghouat (Algeria), in 2008

where she is currently a professor. Her research interests optimal power flow, Artificial intelligence and optimization techniques.



**Ragab El- Schiemy** was born at Minoufiya, 1973. He received the B.Sc., M.Sc., and Ph.D. degrees in 1996, 2005, and 2008, respectively.

He is an Associate Professor in the Department of Electrical Engineering, Faculty of Engineering, Kafrelsheikh University, Kafr el-Sheikh, Egypt.

His research interests involve power system operation, control, and planning, applications of modern optimization techniques for variant electric power systems applications, renewable sources, and smart grid.

**How to cite this paper:** Aboubakr Khelifi, Bachir Bentouati, Saliha Chettih, Ragab A. El-Sehiemy, "A Novel Hybrid Method based on Krill Herd and Cuckoo Search for Optimal Power Flow Problem", International Journal of Image, Graphics and Signal Processing(IJIGSP), Vol.11, No.9, pp. 1-17, 2019.DOI: 10.5815/ijigsp.2019.09.01