

A Fully Adaptive and Hybrid Method for Image Segmentation Using Multilevel Thresholding

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Abstract— High level tasks in image analysis and understanding are based on accurate image segmentation which can be accomplished through multilevel thresholding. In this paper, we propose a new method that aims to determine the number of thresholds as well as their values to achieve multilevel thresholding. The method is adaptive as the number of thresholds is not required as a prior knowledge but determined depending on the used image. The main feature of the method is that it combines the fast convergence of Particle Swarm Optimization (PSO) with the jumping property of simulated annealing to escape from local optima to perform a search in a space the dimensions of which represent the number of thresholds and their values. Only the maximum number of thresholds should be provided and the adopted encoding encompasses a continuous part and a discrete part that are updated through continuous and binary PSO equations. Experiments and comparative results with other multilevel thresholding methods using a number of synthetic and real test images show the efficiency of the proposed method.

Index Terms— Image segmentation, Multilevel thresholding, Particle swarm optimization, Simulated annealing

I. INTRODUCTION

Multilevel thresholding is an important technique that has many applications in image processing, including segmentation, clustering and object discrimination. It aims to separate the objects and the background of the image into non overlapping regions. Thresholding may require the use of one or more thresholds depending on the number of classes that should be depicted in an image. Therefore, based on this assumption, thresholding methods can be divided into two main categories namely bi-level thresholding and multi-level thresholding. In bi-level thresholding, pixels within an image are classified into two classes that consist of the object class and the background class depending on whether their values are above or below a given

threshold. By extension, multilevel thresholding involves several thresholds to classify pixels into more classes. A good review of bi-level and multilevel thresholding algorithms can be found in [1].

Depending on the way to find the thresholds, both bi-level and multilevel thresholding methods can be divided into parametric and nonparametric approaches. The parametric approach is based on a statistical model of the pixel grey level distribution. Generally, a set of parameters that best fits the model is derived using least square estimation. This typically leads to nonlinear optimization problems that are computationally expensive and time-consuming [2, 3]. In the nonparametric approach, the search of the optimal thresholds is done by optimizing an objective function based on some discriminating criteria such as between class variance [4] and entropy [5].

A large number of thresholding methods have been proposed in the literature in order to perform bi-level thresholding and most of them are easily extendable to multilevel thresholding. Despite the straightforwardness of this extension process, the computational time will increase sharply when the number of thresholds is too high because of the exhaustive searching they perform [6]. This weakness makes the multilevel thresholding methods unsuitable in many applications and explains the need to use faster and robust optimization methods for multilevel thresholding problem [7]. As a consequence, several fast techniques have been proposed in the literature such as recursive algorithms [8]. Huang and Wang [9] propose a two-stage multi-threshold based on Otsu's method. Wang and Chen [10] applied an improved shuffled frog-leaping algorithm to the three dimensional Otsu thresholding. Li and Tam presented a fast iterative implementation for the minimum cross entropy thresholding method [11]. Chung and Tsai [12] proposed a fast implementation of binarization algorithm using an efficient heap and quantization based data structure. A recursive programming technique using the maximum cross entropy was proposed by Yin [13]. Shelokar et al. [14] selected the optimal threshold by minimizing the sum of

the fuzzy entropies. Despite the good results of these methods, they still suffer from the problem of long processing time when the number of threshold increases, due to their iterative process.

This limitation has motivated the researchers to find new optimization methods that require moderate memory and computational resources, and yet produce good results. Therefore, metaheuristics have been used as computationally efficient alternatives to traditional multilevel thresholding methods to solve the multilevel thresholding problem. A metaheuristic is a high-level general purpose search strategy which helps exploring large search spaces in order to find good quality feasible solutions. Metaheuristics have been most generally applied to NP-Complete problems and to other combinatorial optimization problems for which a polynomial-time solution exists but is not practical. Since their apparition, metaheuristics have proven their efficiency in solving complex and intricate optimization problems arising in various fields. The most popular and used ones are the Genetic algorithm (GA) [15], Particle Swarm Optimization (PSO) [16], Differential Evolution (DE) algorithm [17], Simulated Annealing (SA) [18], Artificial Bee Colonies (ABC) Algorithm [19], Bacterial Foraging (BF) algorithm [20] ... etc. Due to their capacity to escape from local optima and their ability to find good quality solutions within a reasonable time, several researchers have applied metaheuristics in multilevel thresholding context. Examples of such attempts include the use of GA algorithm [7, 21, 22, 23], DE algorithm [24, 25, 26], PSO algorithm [27, 28, 29, 30], ABC algorithm [31, 32], BFA algorithm [33]. A good review of metaheuristic algorithms for multilevel thresholding can be found in [34].

Despite the relative efficiency of most of methods in the literature to find the optimal thresholds, they all require the number of thresholds to be specified in advance. However, in many practical cases, it is difficult, even impossible to determine the exact number of thresholds without a prior knowledge. Few algorithms have been designed to automatically determine the suitable number of thresholds. Fuzzy entropy is used in [35] to select automatically the optimal number of thresholds and their location in the image histogram. Yen et al. [36] proposed a new criterion for multilevel thresholding, called Automatic Thresholding Criterion (ATC). This criterion includes a bi-level method that correlates the discrepancy between the original and thresholded image and the number of bits used to represent the segmented image [1, 36]. In this strategy, the histogram image is divided into two more sequentially up to the minimum of the cost function ATC is reached [36]. In each step the distribution with the largest variance is further dichotomized in two more distributions by applying the same bi-level thresholding. A new dichotomization process of the ATC method was proposed in [37].

Although the dichotomization techniques are fast algorithms, they are sub-optimal techniques and so they

do not allow providing the optimal threshold values [7]. The GA presented in [7] determines the threshold number as well as the optimal threshold values. In their method, the wavelet transformation is used to reduce the length of the histogram and the GA algorithm optimizes the ATC criterion. Recently, Djerou et al. proposed in [38] an automatic multilevel thresholding approach, based on Binary PSO algorithm, which uses the Otsu's criterion and the Kapur's entropy as objective function. In [39] author adapts the intelligent water drops (IWDs) algorithm to optimize a modified Otsu's criterion for automatic multilevel thresholding.

PSO is a population-based metaheuristic introduced by Kennedy and Eberhart in 1995 [16] as an alternative to the standard Genetic Algorithm (GA). PSO was inspired by social behavior of bird flocking or fish schooling. Each particle within a swarm searches the solution space for the best solution by changing its position with time according to its own experience, and to the experience of neighboring particles. The main advantages of PSO are its flexibility, its robustness and its inherent parallelism. It has been applied in many kinds of engineering problem widely and has proved its large capability to competing with other classical optimization algorithms [40, 41, 42, 43, 44]. However, observations reveal that the PSO suffers from a premature convergence: it converges rapidly in the early stages of the searching process, but can be trapped in a local optimum in the later stages. To overcome this drawback of diversity loss, different hybrid PSOs with others metaheuristics like SA, GA, DE have been proposed. A good and recent review of hybrid PSO can be found in [45, 46].

In this paper, we propose a new automatic multilevel thresholding technique based on PSO. The new method is able to determine both the appropriate number of thresholds and the appropriate threshold values by optimizing ATC [36]. We adopt AMT-PSOSA (Automatic Multilevel Thresholding with PSO and SA) as an acronym to the algorithm we propose in this paper. AMT-PSOSA uses a new hybrid representation to allow particles to contain different thresholds numbers within a given range defined by minimum and maximum threshold number. Particles are initialized randomly to process different cluster numbers in a specified range and the goal of each particle is to search the optimum number of thresholds and the optimum threshold values. In order to allow PSO jump out of a local optimum, SA is applied to some particles of the swarm if no improvement occurs in their best local fitness during a number of iterations. Thus, at the start of SA most worsening solutions may be accepted, but at the end only improving ones are likely to be accepted. This procedure will help PSO to jump out of a local minimum.

The rest of this paper is organized as follows: Section 2 introduces, briefly, PSO and SA algorithms. Section 3 is devoted to detailed descriptions of AMT-PSOSA. The experimental results are evaluated and discussed in section 4. Finally, conclusions are given in section 5.

II. BACKGROUND

A. Particle swarm optimization

Particle swarm optimization (PSO) is a population-based evolutionary computation method first proposed by Kennedy and Eberhart [16]. It is inspired from the natural behavior of the individuals in a bird flock or fish school, when they search for some target (e.g., food). The PSO algorithm is initialized with a swarm of particles (called potential solutions) randomly distributed over the search area. Particles fly through the problem space by following the current optimum particle and aim to converge to the global optimum of a function attached to the problem.

Each particle i in the swarm is represented by two elements: its current position (p_i), and its velocity (v_i). Its movement through the search space is influenced by its personal best position $pbest_i$ it has achieved so far and the local best value $lbest$, obtained so far by any particle in the neighbors of the particle. When a particle takes all the population as its topological neighbors, the $lbest$ value is a global best and is called $gbest$. If the problem space is D -dimensional and the swarm size is Np , at each iteration t , the particle's new position and its velocity are updated as follows:

$$v_{ij}^t = wv_{ij}^{t-1} + c_1 \times r_1 (p_{best} - p_{ij}^{t-1}) + c_2 \times r_2 (p_{gbest} - p_{ij}^{t-1}) \quad (1)$$

$$p_{ij}^t = p_{ij}^{t-1} + v_{ij}^t \quad (2)$$

where $i = 1, 2, \dots, Np$; $j = 1, 2, \dots, D$

The parameter w is an inertia weight [47] used in order to control the values of the velocity. The inertia weight w is equivalent to a temperature schedule in the simulated annealing algorithm and controls the influence of the previous velocity: a large value of w favors exploration, while a small value of w favors exploitation. As originally introduced in [47], w decreases linearly during the run from w_{max} to w_{min} . c_1 and c_2 are two constants which control the influence of the social and cognitive components such that $c_1 + c_2 = 4$. r_1 and r_2 are two random values in the range $[0,1]$.

The main steps of PSO algorithm are presented in algorithm 1.

The particle swarm optimization approach presented above works on continuous space. However, for some optimization problems, a discrete binary representation is better for the particles than a real representation. To deal with this kind of optimization problems, Kennedy and Eberhart proposed in [48] the Binary PSO (BPSO).

Algorithm 1

Initialize all parameters

Initialize particle's positions and velocities

Set $pbest$ for each particle

Compute $gbest$

repeat

for each particle **do**

 Calculate fitness value

 Update $pbest$ if improvement

end

Update $gbest$

for each particle **do**

 Calculate particle velocity according to (1)

 Update particle position according to (2)

end

until maximum iterations is not attained

BPSO preserves the fundamental concept of the Real PSO algorithm and differ from it essentially in two characteristics: first, candidate solutions consists of binary strings each representing a particle's position vector. Second, the velocity represents the probability of bit p_i taking the value 1.

The position update equation is defined by:

$$p_{ij}^t = \begin{cases} 0 & \text{if } r \geq f(v_{ij}^{t-1}) \\ 1 & \text{if } r < f(v_{ij}^{t-1}) \end{cases} \quad (3)$$

with

$$f(v_{ij}^{t-1}) = \frac{1}{1 + \exp(-v_{ij}^{t-1})} \quad (4)$$

where r is a random value with range $[0, 1]$. To avoid saturation of the sigmoid function in (4), the velocity can be limited in the range $[-V_{max}, V_{max}]$.

Despite the fast convergence of PSO, it has been observed that the PSO algorithm can be trapped in a local minimum. This premature convergence occurs because particles fly to local, or near local, optimums, therefore, the balance between the exploration process (searching of the search space) and exploitation process (convergence towards the optimum) is disturbed. In order to overcome this problem, the PSO technique can be combined with some other evolutionary optimization technique to yield an even better performance [43]. In this paper, PSO algorithm is hybridized with the SA algorithm. The hybrid algorithm takes both of fast searching ability in PSO and the advantages of probability jumping property of SA. Other applications of hybrid PSO and SA algorithm can be found [49, 50, 51, 52, 53].

B. Simulated Annealing (SA) algorithm

The original concept of SA was proposed by American physicist Metropolis et al. [54]. It is inspired from the annealing process in metallurgy, which is a method using heat and controlled cooling of a material to increase the size of its crystals. The heat destabilizes the atoms from their first positions and wanders randomly through states of higher energy. It has observed that when the cooling is slow, it gives the

atoms more chances of finding configurations with lower internal energy than the initial one.

Kirkpatrick et al. gives in [18] a mathematical model of the annealing process and uses this model for finding solutions for combinatorial optimized problems, and was the first literature to successfully utilize SA. The principle of SA is to accept solutions of worse quality than the current solution in order to escape from local optima. The probability of accepting such worst solutions is decreased during the search.

A standard SA procedure begins by generating random initial solution called current solution cs . At the initial stages, SA attempts to replace the current solution cs by random solution cs' that is generated by making a small random change in the current solution cs . The objective function $f(cs')$ of the new solution is calculated and the metropolis acceptance rule is then used to determine if the generated solution should be accepted or not as the new current solution. A move to the new solution cs' is made if it improves the current solution cs that is $f(cs')$ is better than $f(cs)$ otherwise it may be accepted with a probability that depends both on the difference between the corresponding function values $f(cs)$ and $f(cs')$ and also on a global parameter T (called temperature) that is gradually decreased during the cooling process. In rejection case, a new solution is generated and evaluated. Typically this step is repeated until the system reaches a solution that is good enough for the problem, or until a given number of iterations is reached. The probabilistic metropolis acceptance mechanism is defined by the following

$$P = e^{(-\Delta E/T)} \quad (5)$$

where

P : Probability for acceptance.

ΔE : The fitness difference between both the fitness of the new generated solution cs' and the fitness of the current solution cs .

T : Temperature value.

The temperature T is decreases during the search process; at the beginning of the search process, the solutions with the worst fitness value are accepted with a high probability and this probability is gradually decreased at the end of the search process.

The pseudo-code of SA algorithm is given in algorithm 2.

Algorithm 2

Let cs the current solution

Evaluate cs and store its fitness value $f(cs)$

Initialize $best_solution$ with the current solution cs

Initialize T_0 (initial temperature) and T_f (final temperature)

Initialize T to T_0

while $T > T_f$ **do**

for a fixed number of iterations **do**

Generate new solution cs' in the neighborhood of the current solution cs

Evaluate the fitness value of the new solution cs'

$$\Delta E = f(cs') - f(cs)$$

if $\Delta E < 0$ **then** $cs = cs'$

else if $\text{rand}(0,1) < e^{(-\Delta E/T)}$ **then** $cs = cs'$

end

Update $best_solution$ with the new generated solution cs'

end

$$T = \alpha * T$$

End

The SA algorithm has a strong ability to find the local optimistic result. With its jump probability, it can avoid the problem of local optimum, but its ability of finding the global optimistic result is weak. In order to improve the results of SA algorithm, it can be used with other techniques like PSO to improve the results.

III. AMT-PSOSA: THE PROPOSED AUTOMATIC MULTILEVEL THRESHOLDING METHOD

In this section, we describe a new automatic image segmentation algorithm using multilevel thresholding based on a hybridization of PSO with SA.

Given a gray level image I to be segmented into meaningful regions. Let there be L gray level values lying in the range $\{0, 1, 2, \dots, (L-1)\}$. For each gray level i , we associate $h(i)$ which represents the number of pixels having the i^{th} gray level as a value. Therefore, the probability p_i of the i^{th} gray level is defined as $p_i = h(i)/N$

where $N = \sum_{i=0}^{L-1} h(i)$ denotes total number of pixels in the image I .

Suppose image I is composed of $M+1$ regions. Hence, M thresholds, $\{t_1, t_2, \dots, t_M\}$ are required to achieve the subdivision of the image into regions: C_0 for $[t_0, \dots, t_1 - 1]$, C_1 for $[t_1, \dots, t_2 - 1]$, ..., C_M for $[t_M, \dots, L - 1]$, such that $t_1 \leq t_2 \leq \dots t_{M-1} \leq t_M$. The thresholding problem consists in choosing the set of optimal thresholds $(t_1^*, t_2^*, \dots, t_M^*)$ that maximizes an objective function f that is:

$$(t_1^*, t_2^*, \dots, t_M^*) = \text{argmax} (f(t)) \quad (6)$$

where t is a potential solution in the feasible region.

The aim of AMT-PSOSA algorithm is to search both the numbers of thresholds as well as the optimal threshold values using the global search capability of PSO and its fast convergence combined with the efficiency of SA to escape from local minimum.

The framework of the AMT-PSOSA algorithm is given in algorithm 3 below.

Algorithm 3

Initialize all parameters (listed in Table 1)
for each particle X_i **do**
 Initialize particle's position
 Initialize particle's velocities stochastically
 Initialize $pbest$
end
Initialize $gbest$ position and M_{best}
iter \leftarrow 0
while (iter < iter_{max}) **do**
 for each particle X_i **do**
 Update particle velocity
 Enforce velocity bounds
 Update particle's position
 Enforce position bounds
 Evaluate particle's fitness
 Record new $pbest$ value of the particle
 end
 Record new $gbest$ and M_{best}
 Select particles that are evolved by SA
 for each selected particle X_i **do**
 $T \leftarrow T_0$
 $current_solution \leftarrow pbest_i$
 $current_fitness \leftarrow fitness(current_solution)$
 while ($T > T_f$) **do**
 iterSA \leftarrow 0, // iteration of SA algorithm
 while (iterSA < iterSA_{max}) **do**
 Generate $neigh_solution$
 Evaluate $neigh_solution$'s fitness
 if accept ($neigh_solution$) **then**
 $current_solution \leftarrow neigh_solution$
 end
 iterSA \leftarrow iterSA + 1
 Update $pbest_i$ if improvement
 end
 $T = \alpha * T$
 end
 Update $gbest$ position and M_{best}
 iter \leftarrow iter + 1
end
Segment the image using the optimal number of thresholds M_{best} and the optimal thresholds values given by $gbest$.

A. Particle representation

Since in this paper, we have to optimize the threshold values and the number of thresholds, we have chosen to represent the particle with both real values and binary values. The real values are used to select the optimal threshold values which are updated by Real PSO algorithm. Binary values are used to select the optimal number of thresholds using the Binary PSO. The Real PSO and Binary PSO evolve in parallel contribute in the evaluation of the fitness function.

In this representation, a binary mask is associated with each threshold value. The value of this mask determines whether the threshold value is used in the thresholding process or not. The initial population

$Pop = \{X_1, X_2, X_3, \dots, X_{Np}\}$ is made up of Np possible particles (solutions). For a user-defined maximum thresholds number T_{max} , a single particle X_i is a vector of T_{max} binary masks and T_{max} real numbers that represent the T_{max} thresholds values.

For a particle X_i , each probably threshold value t_{ij} ($j = 1 \dots T_{max}$) is associated with a mask γ_{ij} . The threshold value t_{ij} is taken into account if its corresponding mask is set to 1 that is: $\gamma_{ij} = 1$ and discarded otherwise that is $\gamma_{ij} = 0$. Therefore, for each particle, the total number of masks set to 1 gives the number of thresholds M_i encoded in it, that is:

$$M_i = \sum_{j=1}^{T_{max}} \gamma_{ij}$$

For a T_{max} thresholds problem, the position of a particle is formulated as:

$$X_i = (\gamma_{i1}, \gamma_{i2}, \dots, \gamma_{iT_{max}}, t_{i1}, t_{i2}, \dots, t_{iT_{max}})^T, \\ \gamma_{ij} \in \{0,1\}, \text{ and } 0 \leq t_{i1} \leq t_{i2} \leq \dots \leq t_{iT_{max}} \leq L-1 \quad (7)$$

subject to $1 \leq i \leq Np$, $1 \leq j \leq T_{max}$

If after initialization, it is found that no mask could be set to "1" in a particle (all threshold values are invalid), one random mask is selected and set to 1. Thus a valid particle should include at least one mask set to 1 in its position vector.

Two examples of the particle structure in the proposed approach are shown on Figure 1.

$$\begin{array}{c} \overbrace{[0,1,0,1,0]}^{\text{masks field}}, \overbrace{[12, 45, 160, 225, 225]}^{\text{thresholds values}} \\ \overbrace{[1,0,1,0,1]}^{\text{mask field}}, \overbrace{[10, 50, 100, 210, 240]}^{\text{thresholds values}} \end{array}$$

Figure 1. Two examples of the particle structure in the AMT-PSOSA algorithm.

In the first example, particle X_i represents 3 classes (2 thresholds), and the associated thresholds values are 45 and 225. Thresholds values 12, 160 and 250 are invalid and not used to thresholding the image.

In the second example, particle X_i represents 4 classes (3 thresholds), and the associated thresholds values are 10, 100 and 240. Thresholds values 50 and 210 are invalid and not used to thresholding the image.

The position of each particle is changed using the following rule: the threshold values are update using continuous PSO equations whereas the mask field is changed using equations of Binary PSO. In addition the velocity of each particle must lie within the interval [0,1].

B. Population initialization

To generate the initial population of particles, we use in this paper the random generation strategy until all particles in a population are created. Each individual particle X_i of the population is initialized by randomly chosen threshold values within the range $[g_{min}, g_{max}]$, where g_{min} and g_{max} are the minimum and the maximum gray levels in the image, respectively.

$$t_{ij} = g_{min} + rand() * (g_{max} - g_{min}) \quad (8)$$

$(i = 1, \dots, Np \text{ and } j = 1, \dots, T_{max})$

In addition, $M_i (1 \leq M_i \leq T_{max})$ masks are randomly chosen and their values are set to "1".

C. Fitness evaluation

The fitness of a particle indicates the degree of goodness of the solution it represents. In this work the fitness of a particle is computed using the cost function ACT [36].

Let M, ω_i, μ_i , and μ be the number of thresholds encoded in a particle, the probability of the class C_i , the mean grey level of the class C_i and the total mean grey level of the image, respectively:

$$\omega_i = \sum_{j=t_{i-1}}^{t_i-1} p_j, \quad \mu_i = \sum_{j=t_{i-1}}^{t_i-1} j p_j / \omega_i, \quad \mu = \sum_{j=0}^{L-1} j p_j$$

where p_j is the normalized probability at level j

Let σ_w^2, σ_B^2 and σ_T^2 be the within-class variance, the between-class variance and the total class variance, respectively. They are given by the following expressions:

$$\sigma_w^2(M) = \sum_{i=0}^M \sum_{j=t_{i-1}}^{t_i-1} (j - \mu_i)^2 p_j,$$

$$\sigma_B^2 = \sum_{i=0}^M \omega_i (\mu_i - \mu)^2$$

$$\sigma_T^2 = \sum_{j=0}^{L-1} (j - \mu)^2 p_j$$

The ACT function proposed by Yen et al. is defined as follows:

$$F(M) = \rho * (Disk(M))^{1/2} + (\log_2(M))^2 \quad (9)$$

The $Disk(M)$ represents the within-class variance and is defined as:

$$Disk(M) = \sigma_T^2 - \sigma_w^2(M)$$

The first term of $F(M)$ measures the cost incurred by the discrepancy between the thresholded image and the original image. The second term measures the cost resulted from the number of bits used to represent the thresholded image. In this equation, ρ is a positive weighting constant and it is set to 0.8 in this study as

recommended in [36]. The number of thresholds is determined by counting the number of "1" in the mask field of the particle position and the corresponding threshold values are determined accordingly.

The fitness $fitness(M)$ of a particle which encoded M thresholds is defined as:

$$fitness(M) = \frac{1}{F(M)} \quad (10)$$

When the algorithm converges, the found number of thresholds M^* and the corresponding found thresholds values are determined by the particle that has the maximum value of fitness function throughout the entire run.

D. SA-based local search

As a metaheuristic based method, PSO has a strong ability in finding the most optimistic result. Meanwhile, it can be trapped in a local optimum. SA has a strong ability in finding a local optimistic result, but its ability in finding the global optimistic result is weak [52]. Combining PSO and SA leads to the combined effect of two algorithms: the fast convergence of the PSO and its efficient global search and the efficient local search of SA and its ability to avoid local minima, which gives better results.

There are many ways to combine PSO with SA, but the best one is which take advantage of probability jumping property of SA without increasing the computational cost or altering the fast convergence ability of PSO. In this paper, we apply the jump property of SA to the process of updating the local best positions of selected particles in the swarm. Indeed, it would be helpful for the best particles to jump out the local minima, and as a result, the whole swarm would move to better positions. SA algorithm is applied for a particle if it is selected with an adaptive probability P_e as in [22]. Let $gbest$ the global best fitness of the current iteration; \overline{pbest} be the average fitness value of the population and $pbest_i$ be the fitness value of the solution (particle) to be evolved. The expression of probability, P_e is given below:

$$P_e = \begin{cases} k_2 \times \frac{(gbest - \overline{pbest}_i)}{(gbest - \overline{pbest})} & \text{if } \overline{pbest}_i > \overline{pbest} \\ k_4 & \text{if } \overline{pbest}_i \leq \overline{pbest} \end{cases} \quad (11)$$

Here, values of k_2 and k_4 are kept equal to 0.5 [22]. This adaptive probability helps PSO to avoid getting stuck at local optimum.

The value of P_e increases when the fitness of the particle is quite poor. In contrast when the fitness of the particle is a good solution, P_e will be low.

SA starts with a local best solution \overline{pbest} of a selected particle X_i and generates a random neighbor solution using a heuristic strategy. A valid threshold t_{ij}

($\gamma_{ij} = 1$) in X_i is chosen to undergo a perturbation operation with probability equal to 0.2. The threshold value is then modified as follows:

$$t_{ij}^{new} = t_{ij}^{old} + \delta * (g_{max} - g_{min}) \quad (12)$$

where $t_{ij}^{new} \in [g_{min}, g_{max}]$

where t_{ij}^{new} and t_{ij}^{old} represent the new and the old threshold value. δ is a random number between $[-1, 1]$. Thus the solution encoded by the particle is reconfigured, although the number of thresholds belonging to it remains unaltered.

After the SA-based local search is completed, the $gbest$ of the whole swarm should be updated if a solution with better quality is found during the local search.

IV. EXPERIMENTAL RESULTS

In order to assess the ability of the proposed algorithm to determine the number of thresholds and to achieve good quality image segmentation, synthetic and real images (Lena, Pepper, Baboon, Airplane, Hunter and Cameraman) have been used.

Figures 2 and 3 show these test images along with their histograms. All real images are of size (512 x 512) except the Pepper image which is of size (256 x 256).

Experiments have been carried out for several number of thresholds M ranging from 2 to 5. First experiments have been conducted to set the control parameters used in the AMT-PSOSA algorithm. Their values are gathered in Table 1.

The quality of the thresholded image has been evaluated using the uniformity measure defined by the following equation:

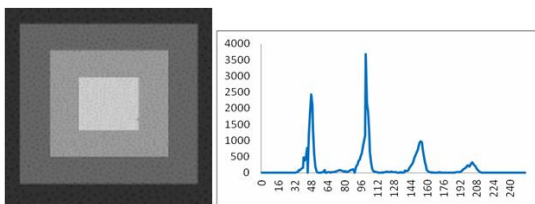


Figure 2. Synthetic image and its histogram.

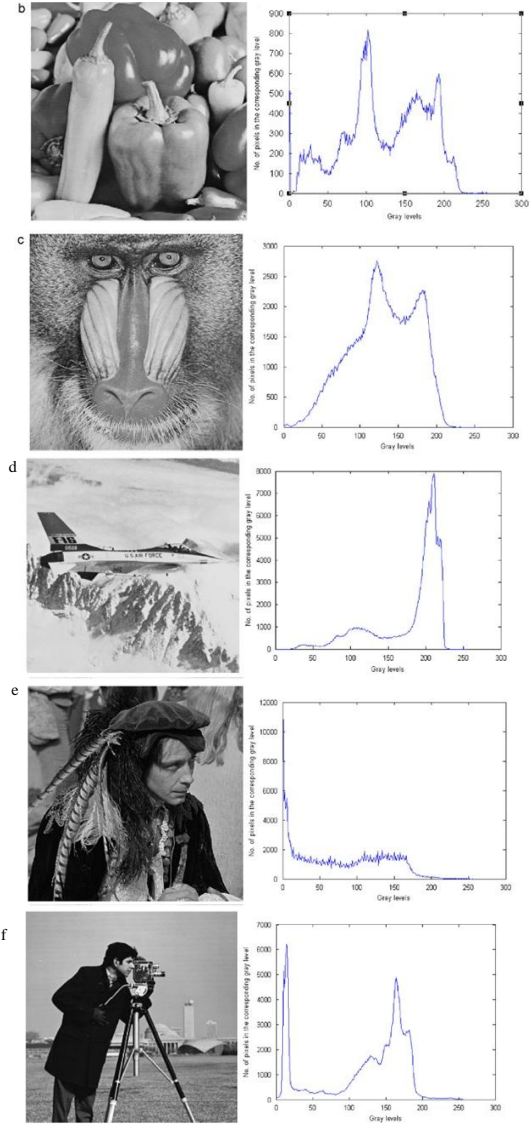
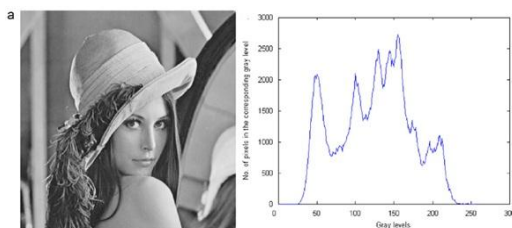


Figure 3. Real test images and their histograms a) Lena; b) Pepper, c) Mandril, d) Airplane, e) Hunter, f) Cameraman

$$U = 1 - 2 * (M) \frac{\sum_{j=0}^M \sum_{i \in R_j} (g_i - \mu_j)^2}{N * (g_{max} - g_{min})^2} \quad (13)$$

Where

- M is the number of thresholds,
- R_j is the segmented region j ,
- g_i is the grey level of pixel i
- μ_j is the mean of grey levels of those pixels in segmented region j
- N is the total number of pixels in the given image,
- g_{max} is the maximal grey level of the pixels in the given image,
- g_{min} is the minimum grey level of the pixels in the given image,

The domain of the uniformity measure is the range $[0,1]$. A higher value of uniformity means that the quality of the thresholded image is better.

TABLE 1. PARAMETER SETTINGS FOR AMT-PSOSA ALGORITHM

Parameters	Values
Population size (Np)	50
Maximum Inertia weight (w_{max})	0.9
Minimum Inertia weight (w_{min})	0.4
Maximum velocity (V_{max})	+1.0
Minimum velocity (V_{min})	-1.0
Cognitive coefficient (C_1)	1.429
Cognitive coefficient (C_2)	1.429
Maximum number of iterations ($iter_{max}$)	1000
// parameter values of SA algorithm	
Initial temperature (T_0)	1000
Final temperature (T_f)	1
Annealing rate (α)	0.99
maximum number of iteration ($iterSA_{max}$)	100

TABLE 2. PARAMETER SETTINGS FOR THE GA AND DMTBPSO ALGORITHMS.

Parameter set for the GA algorithm	Values
Population size (Np)	100
Crossover probability (P_c)	0.9
Mutation probability (P_m)	0.1
Maximum number of iterations	1000
Parameter set for the DMTBPSO algorithm	Values
Population size (Np)	100
P_{ini}	0.5
Inertia weight (w)	0.72
Maximum velocity (V_{max})	255
Cognitive coefficient (C_1)	2
Cognitive coefficient (C_2)	2
Maximum number of iterations	1000

To further appreciate the performance of the proposed method, experimental results from the multilevel thresholding technique based on the recently developed automatic multilevel thresholding algorithm DMTBPSO [38] and on a classical PSO and GA algorithms have been examined and compared with the proposed method AMT-PSOSA. In order to make an objective comparison, the results through an exhaustive search method are also presented. GA-based method, PSO-based method and the exhaustive search method use Otsu's criterion as objective function defined below:

$$f_{Otsu}(M) = \sum_{k=0}^M \omega_k (\mu_k - \mu)^2$$

In the following we will refer to them as ES-Otsu, GA-Otsu, PSO-Otsu and DMTBPSO. Parameter values of GA and DMTBPSO algorithms are presented in Table 2. We employ the best possible parameter settings recommended for DMTBPSO algorithm in [38]. PSO-Otsu is implemented using the same parameter values of AMT-PSOSA.

For GA-Otsu, PSO-Otsu and ES-Otsu, the number of thresholds must be given in advance. In order to compare them with the proposed AMT-PSOSA, we must reformulate them in such a way that the number of

thresholds is extracted automatically. As in [7], GA-Otsu, PSO-Otsu and ES-Otsu are executed in this paper with varying gradually the number of thresholds. The optimal threshold number, which optimizes the cost function ATC defined, is recorded.

The main steps of this algorithm are given in algorithm 4 below [7].

Algorithm 4

1. $M=1$
2. Apply the ES-Otsu method or the GA-Otsu method or PSO-Otsu method using the number M of thresholds
3. Compute the value of the cost function $F(M)$ by using the output optimal thresholds values
4. If $F(M)$ is decreased, set $M=M+1$ and go to step 2 else go to step 5
5. Output the threshold number M^* and the optimal thresholds values obtained from the corresponding multilevel thresholding method.

Moreover, in order to investigate the effects of the hybridization of the PSO with SA, we have compared AMT-PSOSA with a classical PSO based multilevel thresholding method (AMT-PSO) which uses the same particle representation scheme and fitness function as the AMT-PSOSA.

Table 3 summarize the obtained results for the synthetic and real images using the proposed AMT-PSOSA algorithm and the other multilevel thresholding algorithms including the optimal number of thresholds, the corresponding best ATC function value and the uniformity measure related to the synthetic image and the six real test images. Also the computing time of each algorithm is given for each image. From this table, we can draw the following conclusions: The computational time of the exhaustive search method (ES-Otsu) is very expensive and increases sharply when the number of the thresholds increases. AMT-PSO and AMT-PSOSA algorithms provide the same threshold number than GA-Otsu, PSO-Otsu and ES-Otsu algorithms, for all test images. The results of AMT-PSO and AMT-PSOSA algorithms are better than those of DMTBPSO algorithm. AMT-PSOSA is better than AMT-PSO which means that performance is greatly improved by the SA-local search procedure. In most cases, the performance of the proposed method, evaluated through the optimal threshold number M^* , the cost function $F(M)$ and the uniformity measure U , are close to those of ES-Otsu. From computation time view point, the proposed method gives a reasonable CPU time, even though the SA-local search is added.

TABLE 3. COMPARISON OF PERFORMANCES FOR SYNTHETIC AND REAL TEST IMAGE

Image	Algorithms	M*	Thresholds values	ATC function	Uniformity	CPU time
Synthetic image	ES-Otsu	3	74-126-176	6.353374	0.997436	9.897
	GA-Otsu	3	74-126-176	6.353374	0.997436	0.987
	PSO-Otsu	3	74-126-176	6.353374	0.997436	0.645
	DMTBPSO	3	81-125-171	6.513393	0.997218	1.092
	AMT-PSO	3	74-126-176	6.353374	0.997436	0.065
	AMT-PSOSA	3	74-126-176	6.353374	0.997436	0.480
Lena	ES-Otsu	4	75-114-145-180	9.948331	0.991877	5571.872
	GA-Otsu	4	74-112-145-180	9.948545	0.987776	0.987
	PSO-Otsu	4	74-114-145-180	9.948331	0.991877	0.468
	DMTBPSO	4	78-117-150-187	10.04973	0.991598	0.428
	AMT-PSO	4	73-113-146-185	9.950145	0.991750	0.062
	AMT-PSOSA	4	75-114-145-180	9.948331	0.991877	0.420
Pepper	ES-Otsu	4	49-88-129-172	10.742761	0.992231	879.786
	GA-Otsu	4	49-87-129-171	10.744781	0.987543	1.045
	PSO-Otsu	4	50-88-130-172	10.744231	0.991976	0.749
	DMTBPSO	4	52-102-137-168	11.203033	0.991064	0.953
	AMT-PSO	4	49-89-128-171	10.746420	0.992161	0.094
	AMT-PSOSA	4	50-89-129-172	10.743711	0.992168	0.303
Mandrill	ES-Otsu	3	86-124-159	9.599374	0.991805	108.795
	GA-Otsu	3	85-123-158	9.600745	0.986334	1.023
	PSO-Otsu	3	85-124-158	9.599423	0.990754	0.733
	DMTBPSO	3	76-116-155	9.695672	0.991581	0.777
	AMT-PSO	3	84-125-161	9.628662	0.990648	0.047
	AMT-PSOSA	3	86-124-159	9.599374	0.991805	0.688
Jetplane	ES-Otsu	3	89-141-188	9.367949	0.991605	69.218
	GA-Otsu	3	88-140-188	9.377912	0.988023	0.987
	PSO-Otsu	3	89-141-188	9.367949	0.991605	0.577
	DMTBPSO	3	82-143-176	9.821992	0.990456	0.675
	AMT-PSO	3	90-139-186	9.377236	0.991582	0.047
	AMT-PSOSA	3	89-141-188	9.367949	0.991605	0.285
Hunter	ES-Otsu	3	71-114-155	9.951925	0.989024	54.102
	GA-Otsu	3	71-114-155	9.951925	0.989024	0.923
	PSO-Otsu	3	71-114-155	9.951925	0.989024	0.686
	DMTBPSO	4	71-114-149-182	10.16450	0.989953	0.767
	AMT-PSO	3	71-113-155	9.954443	0.989017	0.047
	AMT-PSOSA	3	71-114-155	9.951925	0.989024	0.520
Cameraman	ES-Otsu	3	57-116-154	10.105743	0.992610	113.106
	GA-Otsu	3	59-119-156	10.106754	0.987334	1.023
	PSO-Otsu	3	57-116-154-	10.105343	0.992610	0.702
	DMTBPSO	4	60-110-150-167	10.633063	0.992482	0.876
	AMT-PSO	3	55-114-153	10.106912	0.992608	0.063
	AMT-PSOSA	3	57-116-154	10.105743	0.992610	0.490

As PSO is a stochastic optimization algorithm, the stability of the PSO-based strategies has also been assessed by gathering optimal number of thresholds and the corresponding objective function $F(M)$ values over several runs. The variation of the results through different runs gives an indication of the stability of the used algorithm which is influenced by its search abilities. The more results are close to each other, the more stable is the algorithm. The mean μ and standard deviation σ are defined as:

$$\mu = \frac{\sum_{i=1}^k \sigma_i}{k}, \sigma = \sqrt{\frac{1}{k} \sum_{i=1}^k (\sigma_i - \mu)^2} \quad (14)$$

where k is the number of runs for each stochastic algorithm ($k = 50$), σ_i is the best objective value obtained by the i^{th} run of the algorithm. Higher standard deviation values show that the algorithm is unstable.

TABLE 4. MEAN AND THE STANDARD DEVIATION VALUES OF THE NUMBER OF THRESHOLDS, THE CORRESPONDING OBJECTIVE VALUES AND THE UNIFORMITY MEASURE THROUGH 50 RUNS OBTAINED BY DIFFERENT OPTIMIZATION ALGORITHMS

Images	Algorithms	M*		ATC function		Uniformity	
		mean	deviation	mean	deviation	mean	deviation
Lena	DMTBPSO	4.15	0.589	11.01742	4.7964e-01	0.98969	1.2961e-03
	AMT-PSO	3.75	0.046	10.13291	7.4081e-02	0.99103	6.9339e-04
	AMT-PSOSA	4	0	9.95813	9.1729e-03	0.99185	1.5489e-05
Pepper	DMTBPSO	5.25	0.433	12.24612	3.5860e-01	0.99039	1.2767e-03
	AMT-PSO	3.5	0.049	11.01522	1.1722e-03	0.99101	6.2871e-04
	AMT-PSOSA	4	0	10.75325	1.0666e-03	0.99217	2.4848e-05
Mandril	DMTBPSO	4.06	0.661	10.82737	4.7496e-01	0.99084	1.1987e-03
	AMT-PSO	3.1	0.030	9.63651	3.0049e-05	0.99168	4.2643e-04
	AMT-PSOSA	3	0	9.60531	2.3790e-05	0.99179	1.0138e-05
Jetplane	DMTBPSO	4.05	0.668	10.27023	4.5917e-01	0.99087	1.0525e-03
	AMT-PSO	2.95	0.022	9.44559	4.9994e-03	0.99141	1.1638e-04
	AMT-PSOSA	3	0	9.37127	3.0340e-03	0.99159	7.4358e-06
Hunter	DMTBPSO	4.15	0.572	10.88537	4.6357e-01	0.98791	1.6340e-03
	AMT-PSO	3	0	10.06812	3.0755e-04	0.98871	1.8056e-04
	AMT-PSOSA	3	0	9.95374	2.2595e-04	0.98902	6.6696e-06
Cameraman	DMTBPSO	4.9	0.72	11.44428	3.9183e-01	0.99206	1.1916e-03
	AMT-PSO	2.9	0.061	10.19008	4.1678e-03	0.99265	2.9348e-04
	AMT-PSOSA	3	0	10.10832	4.1132e-03	0.99269	8.0141e-06

The mean and the standard deviation values of the number of thresholds, the corresponding objective values and the uniformity measure through 50 runs for DMBT PSO, AMT-PSO and AMT-PSOSA algorithms has been recorded in Table 4 for the six real test images.

As shown on the Table 4, the proposed algorithm achieves mean values that are closest to optimal ones compared to any of the other strategies. Furthermore, the achieved standard deviation values indicate the superiority of AMT-PSOSA over the other algorithms in terms of stability.

V. CONCLUSION

In this paper, we have proposed a new automatic multilevel thresholding algorithm based on the hybridization of the Particle Swarm Optimization with the Simulated Annealing. The new developed hybrid technique makes full use of the exploration ability of PSO and the exploitation ability of SA and offsets the weaknesses of each. AMT-PSOSA uses both real and discrete values for the particle representation in order to determine the appropriate number of thresholds as well as the optimal threshold values using the ATC function. Experimental results over synthetic and real test images show the efficiency of AMT-PSOSA over exhaustive search method, GA based method, PSO based method and the recently proposed DMTBPSO algorithm.

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