

# Fuzzy Clustering of Sequential Data

**B.K. Tripathy**

VIT, SITE, Vellore-632014, INDIA  
E-mail: [tripathybk@vit.ac.in](mailto:tripathybk@vit.ac.in)

**Rahul**

VIT, SCOPE, Vellore-632014, INDIA  
E-mail: [rahul2014@vit.ac.in](mailto:rahul2014@vit.ac.in)

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**Abstract**—With the increase in popularity of the Internet and the advancement of technology in the fields like bioinformatics and other scientific communities the amount of sequential data is on the increase at a tremendous rate. With this increase, it has become inevitable to mine useful information from this vast amount of data. The mined information can be used in various spheres; from day to day web activities like the prediction of next web pages, serving better advertisements, to biological areas like genomic data analysis etc. A rough set based clustering of sequential data was proposed by Kumar et al recently. They defined and used a measure, called Sequence and Set Similarity Measure to determine similarity in data. However, we have observed that this measure does not reflect some important characteristics of sequential data. As a result, in this paper, we used the fuzzy set technique to introduce a similarity measure, which we termed as Kernel and Set Similarity Measure to find the similarity of sequential data and generate overlapping clusters. For this purpose, we used exponential string kernels and Jaccard's similarity index. The new similarity measure takes an account of the order of items in the sequence as well as the content of the sequential pattern. In order to compare our algorithm with that of Kumar et al, we used the MSNBC data set from the UCI repository, which was also used in their paper. As far as our knowledge goes, this is the first fuzzy clustering algorithm for sequential data.

**Index Terms**—Clustering, Fuzzy Clustering, Sequence mining, Similarity measures, Pattern mining.

## I. INTRODUCTION

Clustering of data is an integral part of Data Mining and serves an important role in many fields such as pattern recognition, scientific data exploration, taxonomy, medicine, geology, business, engineering systems, information retrieval, text mining and image processing. It is a process of grouping data based on their similarity such that elements in individual groups are having more similarity than elements in different groups. There are several approaches to classify the processes of clustering.

With respect to the formation of clusters, it may be hierarchical or non-hierarchical. Hierarchical clustering can further be divided into agglomerative (bottom-up) or divisive (top-down). The additional feature of a sequential dataset in comparison to the normal datasets is the order of occurrence of elements. Sequential data analysis is one of the vital research areas which include deriving better similarity measures, clustering and classification. Several forms of sequential data sets are available; like weblogs, music files, transaction records, and genomic data. There has been an enormous growth in data in various domains including scientific and commercial. These data have inherent sequential nature. Clustering and classification of this sequential data have various applications. As has been found in literature, there have been various methods to classify/cluster sequential data using model-based techniques like the most widely used Hidden Markov models and feature based techniques.

The central problem is the similarity measure that can capture both the content and sequential nature of the items in the given sequential data. In this paper, we will be using kernel-based functions to capture the sequential nature and Jaccard's set similarity measure to capture the content of the sequences. We used fuzzy clustering algorithms to cluster the data into various overlapping clusters based on the similarity or dissimilarity of the sequences.

The rest of the paper is organized as follows. In section 2, a brief literature review along with the problem statement is provided. A new similarity measure called Kernel and Set Similarity Measure ( $KS^2M$ ) is introduced in section 3. In section 4, a brief description of the data set is given that is used for experimentation; also a comparison is made between the new similarity measure  $KS^2M$  and Sequence and Set Similarity Measure ( $S^3M$ ). In section 5, a brief overview of fuzzy set theory and fuzzy clustering algorithms is provided. The proposed algorithm is introduced in section 6. The analysis of the experiment and results obtained are presented in section 7 and we conclude our findings in this paper in section 8.

## II. LITERATURE REVIEW AND PROBLEM STATEMENT

Clustering can be classified on a broader level into hierarchical and non-hierarchical clustering methods. The main difference between the two methods is that in non-hierarchical clustering methods, a desired number of clusters is assumed at the start while in hierarchical methods, a series of successive fusions or divisions are performed based on some external similarity or dissimilarity parameters. Hierarchical clustering methods include agglomerative clustering of data which is bottom-up i.e. starting from single elements or data points they will be merged into a cluster based on some similarity measure, and divisive where the elements/data points are partitioned into smaller partitions (clusters) in the top to bottom manner. Then we have different methods of selecting the data to be clustered like feature based; where we extract some features from the given data and satisfies the following characteristics in the context of sequence mining [35].

1. Effectiveness in capturing the sequential relations between the different set of elements contained in the sequences
2. Wide presence in sequences
3. Completeness of the derived feature space

There are various methods suggested for feature selection or alternatively feature pruning in literature like the global and local approach in [19].

There are several applications of clustering techniques in various real life situations. In [4] a hierarchical clustering method was proposed to handle the attention deficit hyperactive disorder children using attribute dependency. A study on automatic brain tissues segmentation is carried out by using self-initializing k-means clustering technique in [27]. A method to study unstructured activity analysis is proposed by using covering based rough sets in [47]. Clustering techniques have been used successfully in analysis of depth computation of Leukemia images through refined bit plane and uncertainty based models in [42]. Analysis of satellite images provides useful information on the geographical and environmental features of the globe. An attempt in this direction is done in [43]. Big data is a recent revolution in the field of Data Science. A recent volume published in 2017 contains many important contributions on big data classification [40]. Specifically an interesting compilation is made in [47] with up to date information on the different clustering algorithms for big data found in literature so far. Another important algorithm using self-initializing k-means clustering technique is proposed in [27] which do not need any human intervention during the process of brain tissue segmentation. Possibilistic approach to clustering is proposed in [2]. Medoid based clustering algorithms were proposed in [21, 22]. Hybrid clustering approach is dealt in [3].

We also have model-based clustering techniques, the strategies discussed before i.e. feature based and

hierarchical, directly work on the raw data with a definition of the distance or similarity measure or indirectly extract features from the raw data and use the existing clustering algorithms for feature vector based data. The models can be Gaussian, t-distribution for non-sequence data clustering. Among all the possible models, the hidden Markov model (HMM), perhaps the most important one is widely used in speech recognition extensively. We also have other models for sequence clustering like Mixtures of ARMA Models, Mixture of Markov Chains and Mixture of Polynomial models [35].

Along with hard clustering algorithms as mentioned above, in which a particular data point or sequence can only belong to one cluster, Soft clustering algorithms are also there which are based on the principles of the fuzzy set theory [50], rough sets [28]. In soft clustering, a data point or sequence can belong to multiple clusters with a membership value lying in (0, 1) to each cluster.

Work has been done to get Rough overlapping clusters using a Sequence and Set Similarity Measure ( $S^3M$ ) [5], which are defined as:

$$S^3M(A, B) = p * SeqSim(A, B) + q * SetSim(A, B), \quad (1)$$

where  $p + q = 1$

$$SeqSim(A, B) = LLCS(A, B) / \max(|A|, |B|) \quad (2)$$

and  $SetSim(A, B)$  is the Jaccard similarity coefficient given by:

$$J(A, B) = \frac{|A \cap B|}{|A \cup B|} \quad (3)$$

Various comparisons were made between this  $S^3M$  and other similarity measures in [24].

As to be pointed out in the next section, there are some drawbacks of using Length of Longest Common Subsequence (LLCS) to measure the similarity of the order or sequence in a given sequential data. To overcome this problem we have introduced a new similarity measure based on string kernels. The soft clusters obtained by the rough clustering approach don't specify the degree or membership of a particular sequence to different clusters. We develop a fuzzy clustering method that provides us the degree to which a particular sequence belongs to a cluster.

## III. PROPOSED NEW SIMILARITY METRIC

We first start with the main issues which are associated with measures of similarity of two sequences defined through LLCS. The following points need attention:

1. LLCS does not take the position of items into account.
2. LLCS does not consider the length of the part which is not common into account (uses the length to normalize the result.)

We consider the following example to illustrate the above two points. Let us take the three sequences,

$\mathbf{A} = \underline{a}, b, c, d, e$ ,  $\mathbf{B} = q, \underline{a}, e, m, n$  and  $\mathbf{C} = \underline{a}, \underline{e}, t, r, s$ .

The length of the longest common sub-sequence in all three is two; the subsequence being  $\{a, e\}$  irrespective of the location of the items. Intuitively the pair  $\{B, C\}$  should be more similar than  $\{A, C\}$ , and  $\{A, B\}$ . But, LLCS returns the value 'two' for all the pairs.

Jaccard's similarity index is a good similarity index for obtaining the content similarity between given sequences but we can't infer anything about the order of the items/elements in the given sequence.

For example, consider two sequences:  $A = \{1, 2, 3, 4\}$  and  $B = \{4, 3, 2, 1\}$  using the Jaccard's measure the similarity between A and B is '1'; i.e. both are completely similar but from the sequential perspective, the two are completely different as the order of occurrence of elements is in the two sequences is completely different.

On a broader level, we can say that in the similarity measure  $S^3M$ , the first component LLCS is used to get the sequential order from the data and the second component, which is set similarity, is used to get the content of the given data set.

Basing upon the two notes above, we propose that instead of using LLCS, some other better measure can be used, so that it will take into account the position and length of the matching sub-sequence/substring. As a solution to this, we find that Kernel methods for comparing the sequential parts are a good candidate. There are many popular Kernel methods in the literature like Graph kernels, Polynomial kernel, Radial basis function kernel, String kernels as analyzed in [20].

Again, for strings we have various types of kernel methods; like the string sub-sequence kernel (SSK) [26] which allow the gaps or mismatch, whereas some others like the spectrum, compare only exactly matching substrings of the sequences. A nice presentation and analysis on string kernels is provided in [1]. For the sake of completeness, we provide below an overview of some of the commonly used string kernels.

*Spectrum:* This kernel considers only matching the substring of exactly specified length. Each such substring is given a constant weight.

*Boundrange:* This kernel considers only matching substrings of length less than or equal to a given number  $N$ .

*Constant:* This kernel considers all matching substrings and assigns constant weight to each of them.

*Exponential:* Also called exponential decay kernel has the property that the weights of the substrings decay as the matching substring get longer. This kernel requires a decay factor.

It is worth noting that although string kernels take care of the order of the items and to some extent the content (as common substrings are similar in order as well as content); by using only substring matches they ignore the non-sequential part which might be similar in content. So,

it is felt that in order to consider the content of the sequences we can use the same Jaccard's similarity coefficient instead. Both the components; the order of items and their contents are essential as in some applications like web mining, the order of the items is more important/ relevant than the content whereas in some other areas related to bioinformatics the content is more important. Taking into account the above-mentioned factors we propose the following Kernel and  $KS^2M$ .

$$KS^2M(A, B) = p * SK(A, B) + q * J(A, B) \quad (4)$$

where  $p + q = 1$  such that values of  $p$  and  $q$  act as weight factors, and can be varied as per the requirements of the application domain or area. SK stands for any String based kernel we have done used to string kernels one is the Exponential Decay String Kernel from [1] and the other one is String Subsequence Kernel [26] for the sake of comparison between different kernels.

To overcome the limitations of LLCS we used the exponential string kernel in which the substring weight decays as the matching substring gets longer. For example, consider the three random strings:  $x = "abcdeff"$ ,  $y = "agbjckd"$  and  $z = "abncdmv"$ . The matching substring in these strings is "abcd". But a closer look at the sequences says that the similarity between  $x$  and  $y$  should be less than the similarity between  $x$  and  $z$  as the length of the matching substring is seven (agbjckd) in case of  $y$  and that for  $z$  it is five (abncd).

This kernel requires a decay factor [1]  $\lambda > 1$ . The decay factor is used to assign more weight to those substrings in which the length of matching substring is smaller in comparison to those in which the length is larger as explained in the above example of three sequences  $x$ ,  $y$ , and  $z$ .

It is mentioned in [14] that in order to qualify as a good metric, a similarity measure should satisfy the properties of symmetricity, non-negativity and normalized. All these are satisfied by as

$$\text{Symmetric: } KS^2M(A, B) = KS^2M(B, A)$$

Let's take two strings "abcde" and "bc", length of common matching substring taken into consideration by the string kernel is three i.e. to match the common pattern "bc", first three characters of string "abcde" has to be considered. This is symmetric in the sense that the length will remain same for  $KS^2M("abcde", "bc")$  and for  $KS^2M("bc", "abcde")$ .

*Non-negativity:* By its definition,  $KS^2M$  generates non-negative similarity value.

At maximum the value returned by  $KS^2M$  can be zero because the similarity between two strings at worst can be zero i.e. they are completely different strings. There is no meaning of negative similarity in  $KS^2M$  as components, the string kernel, and the Jaccard's similarity

index are based only on the common pattern between two given sequences which can be zero at the minimum for two totally different sequences.

*Normalized:* The value returned by  $KS^2M$  is normalized to lie in the unit interval [0, 1] for better comparison between the different set of sequences.

There are kernels like String Subsequence Kernel (SSK) [28] which takes into account the position of matching substring or subsequence. SSK appears to be too strict on limited length sequential data as shown in the next section.

IV. DESCRIPTION OF THE DATASET AND COMPARISON OF  $KS^2M$  WITH  $S^3M$

Internet Information Server (IIS) logs for MSNBC.com and news related portions of msn.com for the entire day of September 28, 1999, is collected from the UCI dataset repository. Each sequence in the dataset corresponds to page views of a user during that twenty-four hour period. There are 17 page categories, namely 'frontpage', 'news', 'tech', 'local', 'opinion', 'on-air', 'misc', 'weather', 'health', 'living', 'business', 'sports', 'summary', 'bbs', 'travel', 'msn-news', and 'msn-sports'. Table 1 below shows the characteristics of the dataset.

Table 1. Characteristics of the Data Set

Number of users	989,818
Minimum session length	1
Maximum session length	500
Average number of visits per user	5.7

Table 2. Similarity Matrix Using Proposed Metric  $KS^2M$  With P = 0.5

	T1	T2	T3	T4	T5	T6	T7	T8	T9	T10
T1	1.000	0.011	0.006	0.014	0.165	0.245	0.011	0.010	0.041	0.011
T2	0.011	1.000	0.138	0.580	0.208	0.147	0.333	0.152	0.253	0.336
T3	0.006	0.138	1.000	0.151	0.040	0.274	0.528	0.448	0.076	0.334
T4	0.014	0.580	0.151	1.000	0.184	0.075	0.485	0.387	0.267	0.551
T5	0.165	0.208	0.040	0.184	1.000	0.175	0.099	0.063	0.078	0.095
T6	0.245	0.147	0.274	0.075	0.175	1.000	0.203	0.216	0.091	0.182
T7	0.011	0.333	0.528	0.485	0.099	0.203	1.000	0.664	0.228	0.724
T8	0.010	0.152	0.448	0.387	0.063	0.216	0.664	1.000	0.120	0.650
T9	0.041	0.253	0.076	0.267	0.078	0.091	0.228	0.120	1.000	0.262
T10	0.011	0.336	0.334	0.551	0.095	0.182	0.724	0.650	0.262	1.000

In the case of dissimilarities, take any object  $i$  (in our case any sequence) in the data set and denote by  $A$  the cluster to which it has been assigned. When cluster  $A$  contains other objects apart from  $i$ , then we can compute:

$a(i)$ =average dissimilarity of  $i$  to all other objects of  $A$

Now consider any cluster  $C$  which is different from  $A$  and compute:

$d(i, C)$ =average dissimilarity of  $i$  to all objects of  $C$ .

To compare the validity and effectiveness we will be taking the same data samples taken in [26] which consider the following ten random sequences from the above-mentioned dataset of length 6 (as average length is 5.7):

- T1: on-air misc misc misc on-air misc
- T2: news sports tech local sports sports
- T3: bbs bbs bbs bbs bbs bbs
- T4: frontpage frontpage sports news news local
- T5: on-air weather weather weather weather sports
- T6: on-air on-air on-air on-air tech bbs
- T7: frontpage bbs bbs frontpage frontpage news
- T8: frontpage frontpage frontpage frontpage frontpage bbs
- T9: news news travel opinion opinion msn-news
- T10: frontpage business frontpage news news bbs

For the sake of comparison let's cluster them in different clusters using a classic algorithm like Partitioning Around Medoids (PAM)[51] using the similarity matrix generated by  $S^3M$  and by  $KS^2M$ .

We will be using average silhouette width to compare the given similarity measures [33]. Silhouette width value varies between -1 to 1 and in general the greater the value the better are the clusters. The method for the computation of silhouettes as described in [33] is as follows:

Do this for all clusters  $C \neq A$ , select the smallest of those numbers and denote it by  $b(i)$ . Basically what we are looking for is the cluster apart from  $A$  which can be a good candidate or second best choice for the assignment of object  $i$ . Then the number  $s(i)$  silhouette of  $i$  is obtained by combining  $a(i)$  and  $b(i)$  as follows:

$$s(i) = \begin{cases} 1 - \{a(i) / b(i)\}, & \text{if } a(i) < b(i); \\ 0 & , \text{ if } a(i) = b(i); \\ b(i) / a(i) & , \text{ if } a(i) > b(i). \end{cases} \quad (5)$$

when cluster A contains only a single object it is unclear how  $a(i)$  should be defined and then it is simply set to zero, as a value of zero appears to be most neutral. As mentioned earlier, we can easily observe from the above definitions that  $-1 \leq s(i) \leq 1$  for each object  $i$ . In case similarities are used then the same definition can be used with slight modifications as explained in [33].

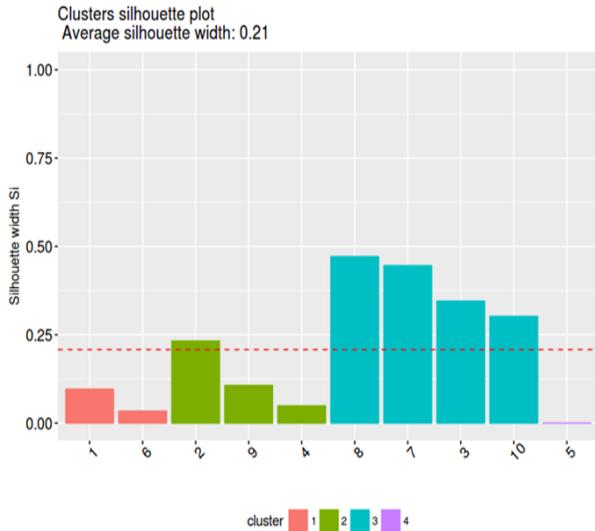


Fig.1. Cluster Silhouette plot with  $k = 4$  using  $KS^2M$  ( $\lambda = 1.3$ ) similarity measure

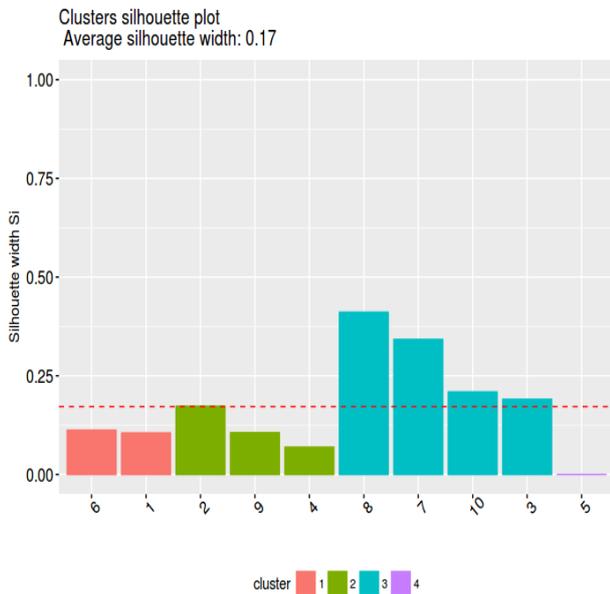


Fig.2. Cluster Silhouette plot with  $S^3M$  similarity measure with  $k=4$  and  $p=0.5$

As is clearly visible from the silhouette plots, average silhouette width value (greater the better) is greater when  $KS^2M$  it is used as similarity measure instead of  $S^3M$  leading to the conclusion that  $KS^2M$  is comparable to  $S^3M$ . Similar results were obtained when compared with a larger number of transactions.

In the next section, a brief overview of Fuzzy sets and fuzzy clustering is presented, to put our proposed

algorithm in the proper perspective. The reason for developing a soft clustering technique like fuzzy clustering instead of hard clustering is that the elements of sequential data sets might be similar to each other, some are more similar and some are less. For example, let's take the  $A = \{a, b, c, d, e, f\}$ ,  $B = \{b, c, d, e, g, h\}$ , and  $C = \{e, g, h, j, k, l\}$ . The similarity of the pair of sequences A and B is higher than that of the pair B and C, as A and B have common sequential part  $\{b, c, d, e\}$  of length four; whereas B and C have the common sequential part  $\{e, g, h\}$ , which has length three. So, similarities of sequences are graded and also the clusters formed have common elements. Hence, scenarios like this can be taken care in a better way by soft clustering methods than hard computing algorithms.

### V. FUZZY SET AND CLUSTERING

Uncertainty in data has become an inherent issue in modern-day datasets. To handle such uncertainty many uncertainty based models have been proposed over the years. Fuzzy set theory introduced by Zadeh in 1965 [49] is one of the most fruitful of such methods. In contrast to dichotomous nature of crisp sets where an element may be in a set or may not be in it, fuzzy set permits graded membership of elements in it. A fuzzy subset X of a universal set U is given by a function  $\mu_x : U \rightarrow [0, 1]$  such that  $\forall x \in U, \mu_x(x) = \alpha \in [0, 1]$ .

Extending the notion of non-membership value of elements in a fuzzy set, the notion of non-membership functions was introduced by Atanassov in [4]. It captures the uncertainty in data in a more realistic manner. Fuzzy set theory for cluster analysis was first proposed in Bellman et al [5] followed by the fuzzy c-means (FCM) algorithm in Ruspini [36-38]. The objective function approach to fuzzy c-means started by Ruspini [37]. This was followed by its improvement by Roubens [33], as the objective function in [36] was complicated and difficult to interpret. But, the objective function in [33] was unstable and Libert and Roubens [25] tried to modify it. This trend was followed by modification of objective functions in Hathaway et al [12, 13] and Bezdek et al [9, 10]. An iterative algorithm which is a variation of the coordinate descent method was described in [35]. But, perhaps the FCM what is used now a day has its origin in the paper by Dunn [13], which was generalized by Bezdek [6]. This method is widely used and applied in a variety of substantive areas. Rough sets were introduced by Pawlak in 1982 [30]. The above approach is now followed extensively in developing clustering algorithms which are either extension like intuitionistic fuzzy C-means (IFCM) [12] and the hybrid algorithm of rough fuzzy c-means (RFCM) [28, 29, 31] and the rough intuitionistic fuzzy c-means (RIFCM) [11]. It may be noted that several generalized versions of FCM exist in the literature [7, 8, 15, 17, 36, 48, 50]. However, there are no fuzzy algorithms to cluster sequential data available in the literature [32]. In this paper, our attempt is to develop a fuzzy clustering algorithm for sequential data.

Variants of fuzzy set based or its hybrid models have been used in developing clustering algorithms to handle specific situations in data analysis. For example Hu et al [24, 27] have extended fuzzy clustering to ordinal scale and further by using likelihood functions. Genetic algorithms are now well-known methods to handle optimization situations. Using particle swarm optimization (PSO) an efficient clustering algorithm is proposed in [5]. Incomplete data sets are common in modern societies due to various reasons. Handling such data sets have been dealt with from different angles. A fuzzy clustering algorithm is proposed in this direction in [26]. A Clustering technique has been proposed in [47] which deals with unstructured activity analysis using the generalised notion of covering rough sets. Graph clustering algorithms are relatively rare in the literature. A brief account of such algorithms based on FMST with a comparative analysis is found in [39]. Datasets may be heterogeneous, i.e. they may contain categorical and nominal attributes together. Several algorithms have been developed in the literature to handle clustering of such data sets using rough set theory. The latest one which generalises the family of such algorithms is presented in [45], called the Min Mean Mean Rough set clustering algorithm (MMeMeR), which has been found to be the most efficient and the authors have observed that this algorithm if extended by using existing techniques followed in the family of algorithms leading to this does not provide any improvement in the clustering process. An adaptive clustering approach is provided in [16] and an application to medical diagnosis is provided in [15, 41].

## VI. MOVING TOWARDS THE FUZZY CLUSTERS

The c-means algorithms (hard or fuzzy) are popular and effective tools in order to cluster  $n$  objects into groups of similar individuals for data available as a set of  $n$  feature vectors in  $RP$ . It may be noted that for data sets described in terms of relational data cannot be handled by these algorithms directly [18, 48, 49]. There are various algorithms in the literature to handle relational data for fuzzy clustering including the "Relational dual of the c-means clustering algorithm" [18] which is the dual of the most widely used Fuzzy c-Means algorithm. There are some constraints on using these algorithms, some require that the distance or similarity(dissimilarity) measure should be derived from the Euclidean distance[RFCM]. To overcome this distance measure constraint a new algorithm NERFCM which involves extra computations for data expansion(Beta-spread transformation) was introduced [18].

We will be using a variant of FANNY(by Kaufman and Rousseeuw) [23], which is extended by Martin M. et al [27] to allow user-specified parameters like the value of fuzzifier ( $m$ ), which is fixed to 2 in the original algorithm. It is more robust to spherical cluster assumption and also provides a novel graphical display, the silhouette plot. When compared to the likes of Fuzzy C-means, FANNY is a bit slower as in each iteration

cycle FANNY performs a loop over all the pairs of objects and in case of Fuzzy C-Means the looping is over the measurement variables and the number of objects is normally more than double of the number of variables. In the improved algorithm the following objective function is to be minimized:

$$\sum_{p=1}^k \frac{\sum_{i,j=1}^n \mu_{ip}^m \mu_{jp}^m d(i,j)}{2 \sum_{j=1}^n \mu_{jp}^m} \quad (6)$$

Here, the membership of the  $i^{\text{th}}$  object to cluster  $p$  is represented by  $\mu_{ip}$ . It may be noted that the numerator of the objective function contains dissimilarities  $d(i, j)$  and the membership coefficients to be determined and the sum is over all pairs of objects unlike objective functions of other algorithms which contain the sum of distances of objects from cluster centres. The factor '2' in the denominator takes care of distances between a pair of objects being counted twice because of similarity.

To measure the fuzziness of the clusters we have used the Dunn's partition coefficient (1976) given by

$$F_k = \sum_{i=1}^n \sum_{p=1}^k \frac{\mu_{ip}^2}{n} \quad (7)$$

The expression in (4) assumes the minimal value  $1/k$ , 1 when the clustering is complete and the maximal value '1' occurs for crisp partitioning. The normalized version  $F'_k$  is given by

$$F'_k = \frac{kF_k - 1}{k - 1} \quad (8)$$

and ranges between 0 and 1. In the next section, the overall outline of the algorithm is given, which is used for clustering of the above-mentioned datasets.

### A. Algorithm for Fuzzy Clustering of Sequential Data

Fanny requires the dissimilarity matrix or the pairwise dissimilarity of the given objects. The clustering algorithm is free from the distance or similarity metric used to generate the pairwise similarity. Here, we use the  $KS^2M$  similarity metric to generate the similarity matrix, then to obtain the entries of the dissimilarity matrix we take the 1's complement of corresponding entries in the similarity matrix, which provides us the respective pairwise dissimilarity. The dissimilarity matrix is required because FANNY starts with a collection of dissimilarities and doesn't depend upon any other measure. Overall, the detailed description of the algorithm is as follows:

**Algorithm:** Fuzzy Clustering of Sequential data

**Input:**

T: A set of  $n$  transactions  
 K: No. of clusters  
 m: Fuzzifier value  
 tol: tolerance value  
 max\_it: Maximum no. of Iterations

**Output:**

K number of overlapping clusters  
 V: normalized Dunn's partition coefficient  
 P: a silhouette plot for each transaction/sequence.

**Begin:**

Step 1: Construct the similarity matrix ( $sim\_m$ ) using  $KS^2M$  measure.

Step 2: Construct dissimilarity ( $diss$ ) matrix by taking 1's complement of  $sim\_m$ .

Step 3: while (not converged and iterations < max\_it):  
     fanny( $diss, k, m, max\_it, tol$ )

Step 4: Return K clusters.

**End**

Using the cluster data we can also calculate the values of Silhouette plot (P) using equation 2 and Dunn's partition coefficient (V) using equations 3 & 4. As mentioned earlier Silhouette width is used as a measure of cluster validation the more it is the better the clustering and Dunn's partition coefficient is used to measure the fuzziness of the clusters formed the less the value the more fuzzier the clusters. The algorithm will terminate in two scenarios, one in which the convergence is reached i.e. the difference between the value of the objective function (3) for two consecutive iterations is less than the tolerance value and the other when the algorithm is not converged but the maximum no. of iterations is reached. Both the tolerance value and the maximum no. of

iterations are given as input parameters.

In the next section, the above-mentioned algorithm is used on variable sizes of the dataset. While performing the experimental analysis, it was observed that sometimes the computation time for more transactions (sequences) is less as compared to a smaller number of transactions i.e. the number of iterations needed is smaller for the prior. The time complexity of FANNY cannot be computed or hard to do so as the data size determines the number of iterations. One can go through chapter 4 of [25] for the detailed explanation of FANNY along with its similarities to other fuzzy clustering algorithms like Fuzzy c-means and others.

## VII. EXPERIMENTAL RESULTS

We have conducted experiments on data sets of variable size ranging from ten to three thousand randomly selected transactions. Results obtained are summarized in Table 5. For the better selection of the number of clusters we have used the average Silhouette width as a cluster validation factor; that is, we have selected the number of clusters as the value of the maximum average silhouette width for a given set of inputs. This is shown in Fig. 3.

The clusters obtained are overlapping clusters i.e. each transaction is assigned to different clusters with different memberships. To have a look at the structure of the clusters formed, we present the results of fifty randomly selected transactions. The categories are labelled with integers; like labels of 'frontpage' and 'news' are '1' and '2' respectively. The hits of a user are presented in the rows of Table 4.

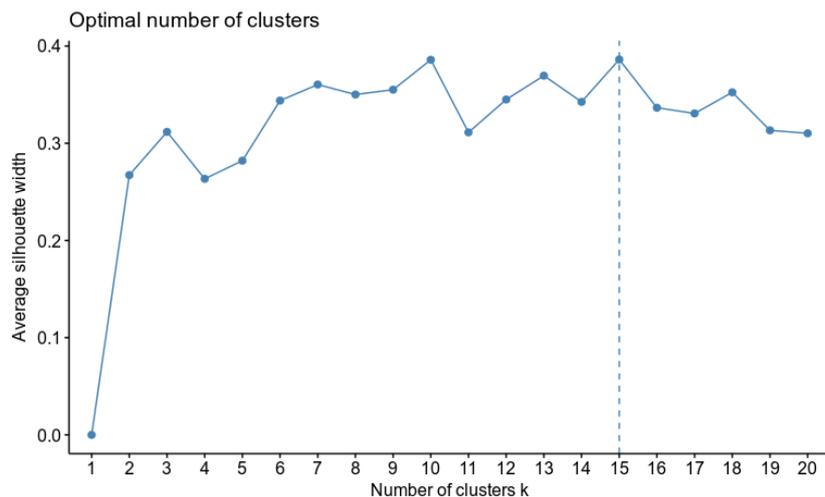


Fig.3. Computation of the no. of clusters using average Silhouette width for transactions listed in Table 3

Table 3. Sample of Fifty Web Transactions

1	('3', '2', '2', '4', '2', '2')	26	('6', '2', '2', '2', '15', '2')
2	('6', '7', '7', '7', '6', '6')	27	('1', '14', '1', '14', '1', '1')
3	('6', '9', '4', '4', '4', '10')	28	('9', '7', '7', '9', '4', '4')
4	('8', '8', '1', '7', '8', '8')	29	('1', '14', '14', '14', '14', '14')
5	('13', '7', '13', '7', '7', '13')	30	('1', '1', '14', '1', '14', '14')
6	('13', '8', '13', '13', '13', '14')	31	('8', '8', '8', '8', '8', '8')
7	('13', '13', '13', '13', '13', '13')	32	('1', '1', '11', '11', '11', '1')
8	('1', '1', '11', '1', '12', '1')	33	('9', '9', '13', '13', '13', '13')
9	('14', '14', '14', '14', '14', '14')	34	('6', '6', '6', '15', '5', '6')
10	('9', '12', '9', '9', '9', '9')	35	('1', '3', '3', '1', '1', '1')
11	('1', '2', '1', '14', '14', '14')	36	('1', '1', '10', '1', '1', '1')
12	('1', '4', '7', '1', '10', '10')	37	('9', '9', '9', '4', '4', '4')
13	('1', '1', '4', '10', '10', '10')	38	('4', '4', '4', '4', '4', '4')
14	('8', '8', '8', '8', '8', '8')	39	('6', '6', '6', '6', '6', '6')
15	('9', '7', '9', '7', '7', '9')	40	('8', '8', '14', '14', '14', '4')
16	('4', '4', '10', '10', '10', '10')	41	('9', '7', '9', '5', '5', '5')
17	('8', '8', '8', '8', '8', '13')	42	('1', '2', '1', '2', '1', '6')
18	('1', '1', '1', '12', '1', '10')	43	('9', '3', '4', '6', '7', '7')
19	('13', '13', '13', '13', '13', '13')	44	('9', '5', '5', '5', '5', '5')
20	('13', '13', '13', '14', '14', '14')	45	('1', '11', '17', '1', '1', '6')
21	('5', '5', '5', '5', '5', '5')	46	('12', '12', '12', '14', '14', '14')
22	('11', '1', '1', '1', '2', '1')	47	('13', '13', '13', '13', '13', '13')
23	('8', '8', '8', '8', '8', '8')	48	('1', '14', '14', '14', '14', '1')
24	('9', '9', '9', '9', '9', '5')	49	('1', '6', '6', '10', '10', '10')
25	('1', '2', '2', '2', '2', '2')	50	('12', '12', '12', '12', '12', '12')

No. of clusters (k) =15

Tolerance =1e-5

p = 0.6, q = 0.4 (order of the sequence is given more weight) m = 1.7

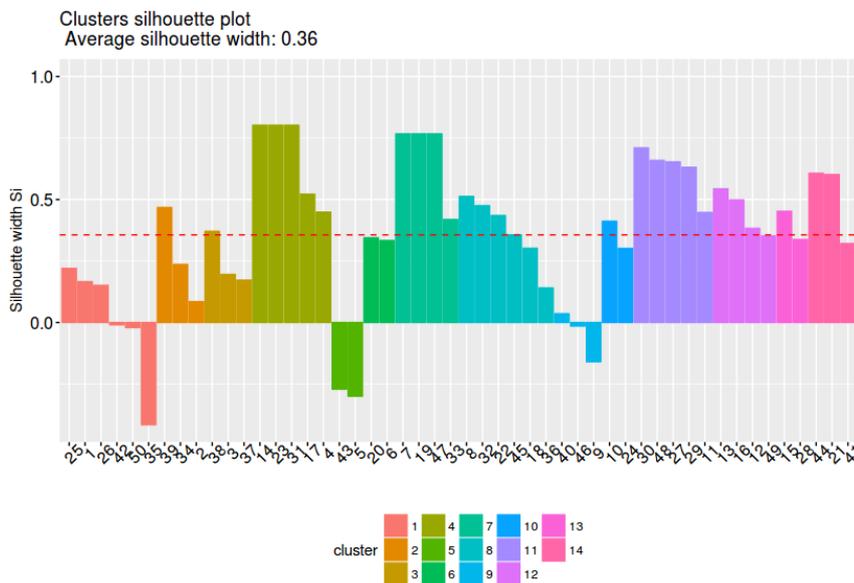


Fig.4. Cluster Silhouette plot with k=15 using the  $KS^2M$  similarity measure

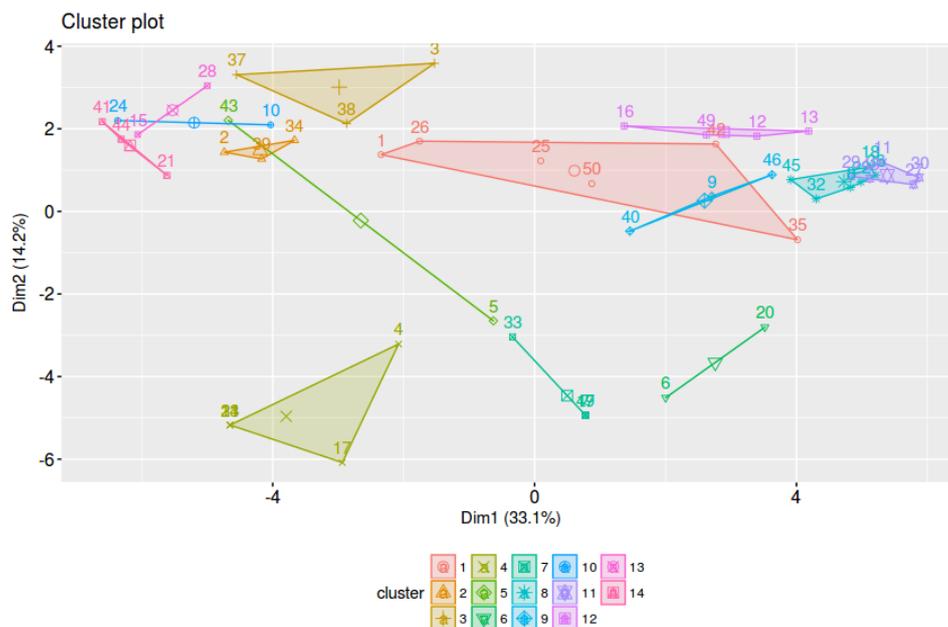


Fig.5. Crisp cluster plot of the transactions in Table 2

*Underlying cluster structure:* As we have used fuzzy clustering algorithms, the clusters should have an overlapping structure i.e. one transaction can belong to various clusters with varying membership values lying in (0, 1). A crisp cluster plot can be shown by assigning the data sequences to those clusters in which they have the

maximum membership value, the tie is broken by selecting anyone cluster randomly, such a plot is shown in Fig. 5. In Table 4 we have listed the degrees of belongingness of the first 10 transactions from Table 3, to 15clusters.

Table 4. Membership Values of First Ten Transactions

	C1	C2	C3	C4	C5
T1	0.1247107547	4.786556e-02	6.306157e-02	4.150351e-02	0.1247107547
T2	0.1017356296	1.279904e-01	6.065663e-02	3.979379e-02	0.1017356296
T3	0.0083193159	4.042299e-03	9.301986e-01	2.620698e-03	0.0083193159
T4	0.1062574976	4.283117e-02	4.715071e-02	1.190521e-01	0.1062574976
T5	0.1085935313	4.055198e-02	4.606384e-02	3.515933e-02	0.1085935313
T6	0.0104532972	3.597261e-03	4.435396e-03	4.195599e-03	0.0104532972
T7	0.0001727610	6.942278e-05	7.907199e-05	6.127987e-05	0.0001727610
T8	0.0644565646	1.475648e-02	1.780729e-02	1.274614e-02	0.0644565646
T9	0.0118194561	4.261906e-03	6.505562e-03	3.719402e-03	0.0118194561
T10	0.0945576283	4.018902e-02	5.780429e-02	3.502571e-02	0.0945576283

	C6	C7	C8	C9	C10
T1	5.547569e-02	4.433506e-02	5.948177e-02	5.596454e-02	4.890683e-02
T2	4.861291e-02	3.972324e-02	5.263081e-02	4.877193e-02	4.661362e-02
T3	3.796023e-03	2.818474e-03	4.037273e-03	4.761592e-03	4.031263e-03
T4	6.109563e-02	3.968123e-02	6.427554e-02	5.020444e-02	4.333372e-02
T5	9.241485e-02	9.259198e-02	6.178594e-02	5.153410e-02	4.095466e-02
T6	9.060171e-01	1.404459e-02	6.199910e-03	7.163494e-03	3.657663e-03
T7	3.330332e-04	9.983418e-01	1.089503e-04	9.114765e-05	7.050041e-05
T8	2.354641e-02	1.719810e-02	5.890399e-01	2.274222e-02	1.503953e-02
T9	8.445114e-03	4.426664e-03	6.770689e-03	8.814046e-01	4.335732e-03
T10	4.627521e-02	3.730241e-02	5.513418e-02	4.623465e-02	1.711853e-01

	C11	C12	C13	C14	C15
T1	4.858132e-02	6.107853e-02	5.058996e-02	4.902339e-02	0.1247107547
T2	4.324751e-02	5.211687e-02	8.672480e-02	4.791062e-02	0.1017356296
T3	4.113494e-03	6.988868e-03	4.110347e-03	3.523083e-03	0.0083193159
T4	5.266665e-02	5.980031e-02	5.694969e-02	4.418633e-02	0.1062574976
T5	4.754302e-02	5.763058e-02	6.618988e-02	4.179925e-02	0.1085935313
T6	6.235334e-03	5.658205e-03	3.758548e-03	3.677021e-03	0.0104532972
T7	8.445117e-05	9.891202e-05	7.216886e-05	7.101965e-05	0.0001727610
T8	3.006254e-02	3.339625e-02	1.527503e-02	1.502042e-02	0.0644565646
T9	2.872958e-02	7.121539e-03	4.463450e-03	4.357355e-03	0.0118194561
T10	4.134532e-02	4.830115e-02	8.335657e-02	5.417334e-02	0.0945576283

Table 5. Experimental Results

No. of data samples	No. of overlapping Clusters(k)	Fuzzifier(m)	Average Silhouette Width	P	Normalized Dunn's Partition coefficient
10	4	1.96	0.20	0.5	0.26
25	9	1.85	0.27	0.5	0.33
50	18	1.8	0.22	0.5	0.42
250	78	1.8	0.26	0.5	0.47
500	136	1.8	0.30	0.5	0.48
1000	187	1.7	0.28	0.5	0.44
2000	430	1.6	0.36	0.5	0.53
3000	515	1.7	0.39	0.5	0.50
3000	550	1.6	0.40	0.5	0.51

#### A. Result analysis

When the object set is increased in size, its dimension also goes up. It has been observed that the value of the fuzzifier  $m$  needs to be decreased so that proper clustering can be achieved. But robustness of a clustering algorithm varies directly as the value of  $m$ . As clearly visible from Table 6, the value of  $m$  has decreased from the maximum 1.96 to a minimum of 1.6 as the sample size increases from 10 to 3000.

Normalized Dunn's partition coefficient is used to measure the degree of fuzziness of the clusters formed. The value of Dunn's coefficient lies between 0 and 1, a value nearer to 1 represents crisper clusters while a value close to zero represents less crisper i.e. more fuzziness in the clusters formed. The value of this coefficient should increase as we decrease the value of fuzzifier ( $m$ ), as the degree of fuzziness is controlled by the value of fuzzifier. There is no fixed value of fuzzifier that should be used, generally, a value between [1.5, 2.5] is suggested for obtaining fuzzy clusters [6]. We have used the same range for our experimental analysis. As clearly visible from the Table 6, the value of Dunn's coefficient agrees with our above observation between same data samples (3000 at 1.7 and 1.6) as well as between different data samples.

We have kept equal weightage for both parts the sequence and the content which can be varied as per the requirement of the domain as mentioned earlier, in some domains related to bioinformatics, the content is more important in that case the value of  $p$  can be decreased while in some domains related to web mining the sequence or order of items is more important in that case we can increase the value of  $p$ .

The algorithm used is stable can be established by the fact that the value of average silhouette width is always

above 0.25 in most of the cases. In fact, as visible from Table 6, the value starts increasing as we increase the no. of data samples. The value of average silhouette width as mentioned earlier ranges between [-1, 1] and measures how good a given data sample belongs to its own cluster in comparison to the nearby clusters. The greater the value the good the clusters formed. The reason why we have used average silhouette width along with Dunn's partition coefficient as a measure of cluster quality is that both of these two indices are used in the original algorithm as described in [23][24].

## VIII. CONCLUSIONS

In this paper, we applied the concept of fuzzy clusters to classify different sequential patterns in different groups based on the sequence as well as content similarity. We introduced a new similarity measure  $KS^2M$  which in comparison to other similarity measures like cosine similarity, Jaccard's similarity index and  $S^3M$  captures the order and the content of the elements/items in the sequences more appropriately. In  $S^3M$ , LLCS is used which has some limitations as mentioned above.

We have obtained overlapping clusters similar to what is obtained in [24] but the main difference lies in the specification of the degree (membership) of a particular sequence to a particular cluster instead of only the no. of overlapping clusters, a sequence or pattern belongs to. We would like to note that an integrated covering based rough fuzzy set based clustering algorithm was developed in [44] for sequential data which extends the algorithm proposed in [24].

Different initial membership matrices will lead to different cluster structure, here we used a random initial

membership matrix, and work can be done in future to improve this initial membership matrix to obtain more meaningful clusters. We have used silhouette width as an index to get a rough estimate of the number of clusters ( $k$ ), other methods like analysis of kernel matrix; elbow method etc. can be compared to obtain an appropriate estimate of the value of  $k$ .

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interests include Fuzzy Set Theory and Applications, Rough set Theory and Knowledge Engineering, Multiset theory and its Applications, Social Networks Analysis, Granular Computing, Soft Computing, Data Clustering Techniques and Applications, Content Based Learning, Knowledge Representation and Reasoning, Soft Set Theory and Applications, Neighbourhood Systems, Information Retrieval, Big Data Analytics, Social Internet of Things and Multicriteria Decision Making.



**Rahul Dahiya** is pursuing his B.Tech in Computer Science and Engineering from VIT University. His interests lie in the fields related to Data Mining, Soft Computing, Machine Learning and Big Data Analytics.

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## Authors' Profiles



**B.K. Tripathy** is a Senior Professor and Dean in the School of Information Technology and Engineering, VIT, Vellore, India. He has published around 530 technical papers in International Journals/Proceedings of International Conferences/Edited book chapters, published 7 books and a monograph. He

has guided 29 PhDs, 13 MPhils and 5 M.S candidates so far. Dr. Tripathy is a senior/ life member of ACM, IEEE, IRSS, CSI, OMS.OITS, IACSIT, IST and IMS. He is a reviewer/ editorial board member of 80 international journals. His current research