

# Application of GA for Optimal Location of FACTS Devices for Steady State Voltage Stability Enhancement of Power System

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**Abstract**— This paper presents a non traditional optimization technique, genetic algorithm to seek the optimal allocation, type and size of FACTS devices to control line flows, to maintain bus voltage to desired level and to minimize system losses. The targeted objectives are maximizing the static security margins and voltage stability while minimizing losses. Congestion management is also done by optimally placing FACTS controllers with line outage. Matlab coding has been developed for the purpose of simulation. Assessments are done on IEEE 30 bus system against different loading conditions with two FACTS devices SVC and TCSC implemented in steady state and the results verify the potency of propound algorithm to find the optimal location for power system stability.

**Index Terms**— FACTS, TCSC, SVC, Genetic

## I. Introduction

The power electronics technology development gives good opportunities to design new power system equipment for power system stability. FACTS technology has become a very effective means to improve capacity of existing power transmission network without the necessity of adding new transmission lines. These devices control the power flow by reducing the power flow in overloaded lines and reduce line losses [1-3].

To achieve good performance of these devices it is important to ascertain their location because of their significant costs. Several methods are used for finding out the location of these devices in an integrated system but various complications are involved and also the results obtained are not optimal in some cases [4, 5]. The issue of optimal location of FACTS devices has been extensively brainstormed and several strategies have been proposed and implemented, but most of the

research is based on the optimization of single objective like voltage stability, loss reduction or cost minimization [6-8]. Some of the researchers have factored in the cost of generator and the cost of installation of FACTS devices to reach at the total cost of the system [9]. Optimal location of FACTS devices for reducing the total cost has been discussed in [13]. In [15] congestion management has been done by taking branch loading as objective function. In [16] a PSO based approach has been discussed to find the optimal location of FACTS devices to improve loadability and reduce the overall cost of installation. Different type of FACTS devices and their locations have different advantages, so the type, rating and location have to be determined simultaneously. This concurrent optimization can be done with genetic algorithm.

This paper presents a genetic based method to seek the type, rating and best location of FACTS controllers to maximize the branch loading and voltage stability reducing the overall system losses. Congestion management is also done by optimally placing FACTS controllers.

## II. Problem Formulation

The stability problem is to optimize the steady state performance of a power system in terms of one or more objective functions while satisfying various equality and inequality constraints.

### 2.1 Objective Functions

Voltage Level (VL):

This objective function takes voltage levels into account. For voltage levels between 0.9 to 1.1 p.u, the value of objective function is equal to 1. Outside this range, the value decreases exponentially with the voltage deviation [16].

$$VS = \begin{cases} 1 & ; \text{if } 0.9 < V_b < 1.1 \\ \exp(\mu |1 - V_b|) & \text{otherwise} \end{cases} \quad (1)$$

Maximize branch loading

The objective function is associated with line loading and penalizes overloads in the lines. This term, called OVL is calculated for every line of the system. While the branch loading is less than 100%, its value is equal to 1: then it decreases exponentially with the line overloading. To speed up the convergence, the product of all objective functions is taken [15, 16]

$$\text{Branch loading} = \sum_{\text{line}} OVL_{\text{Line}} \quad (2)$$

$$OVL = \begin{cases} 1 & P_{pq} < P_{pq \max} \\ \exp\left(\lambda \left|1 - \frac{P_{pq}}{P_{pq \max}}\right|\right) & P_{pq} > P_{pq \max} \end{cases} \quad (3)$$

Where OVL is line overload factor.

#### Loss Minimization

The objective is to minimize the system losses [17]

$$P_L = \sum_{k=1}^{nl} gk \sqrt{V_i^2 + V_j^2 - 2V_i V_j \cos(\delta_i - \delta_j)} \quad (4)$$

## 2.2 Problem Constraints

Equality Constraint

These constraint represent load flow equations as

$$P_{Gi} - P_{Di} - V_i \sum_{k=1}^{nl} V_j [G_{ij} \cos(\delta_i - \delta_j) + B_{ij} \sin(\delta_i - \delta_j)] = 0 \quad (5)$$

$$Q_{Gi} - Q_{Di} - V_i \sum_{k=1}^{nb} V_j [G_{ij} \sin(\delta_i - \delta_j) + B_{ij} \cos(\delta_i - \delta_j)] = 0 \quad (6)$$

Where  $i=1,2,\dots,nb$  is the number of buses;  $P_G$  and  $Q_G$  are the generator real and reactive power respectively;  $P_D$  and  $Q_D$  are the real and reactive loads respectively,  $G_{ij}$  and  $B_{ij}$  are the transfer conductance and susceptance between bus  $i$  and bus  $j$  respectively.

*Inequality Constraints*

These represent the system operating conditions such as generator voltage  $V_G$ ; generator reactive power output  $Q_G$ ; transformer tap  $T$ ; switchable VAR compensations  $Q_C$  and load voltages  $V_L$ .

$$V_{Gi}^{\min} < V_{Gi} < V_{Gi}^{\max}$$

$$Q_{Gi}^{\min} \leq Q_{Gi} \leq Q_{Gi}^{\max} \quad i=1,\dots,NG$$

$$T_i^{\min} \leq T_i \leq T_i^{\max} \quad i=1,\dots,NT$$

$$\text{Where } 0.9 \leq T_i \leq 1.0$$

$$0.95 < V_{Li} < 1.05$$

Where  $V_{Li}$  is the voltages of all the load buses.

## III. Proposed Algorithm

The aim of the optimization is to find the best location of FACTS devices to optimize certain objectives. In this paper we use genetic algorithm optimization technique taking location, type and rating as variables. Genetic algorithms are computerized search optimization algorithm based on the theory of natural selection. An individual is represented with three strings of length. The first string represents the values of the devices. It can take discrete values between 0 and 1, 0 corresponding to the minimum value of the device and 1 to the maximum. According to the model of the FACTS, the real value of the device is calculated with the relation.

$$V_{\text{REALF}} = V_{\text{MINF}} + (V_{\text{MAXF}} - V_{\text{MINF}}) \quad (7)$$

Where  $V_{\text{MINF}}$  and  $V_{\text{MAXF}}$  are respectively the minimum and maximum set value of the device, and is its normalized value. The second string is related to the kind of the devices. A value is given to each type of modeled device 1 for SVC, 2 for TCSC. The last string is the location of the devices. It denotes the numbers of the lines where the FACTS are to be placed.

GA starts with random generation of initial population and then the selection crossover and mutation are performed until the best solution is obtained. GA is practical algorithm and very easy to implement in a power system analysis. Various steps to be performed in Genetic Algorithm implementation are as follows.

### 3.1 Encoding

Initial population is generated through encoding. Three parameters are taken namely: the location, type and its rated value. Each individual is represented by  $N$  number of strings, where  $N$  is the number of FACTS devices to be required in the power system, as shown in Figure 1. Here  $N$  is 5.

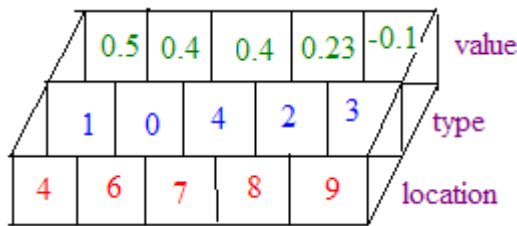


Fig. 1: Individual configuration of FACTS devices

The first string shows the no of lines where the device has to be placed. The second string shows the types of the devices. A value is given to each type of modeled FACTS device: 1 for SVC; 2 for TCSC and 3 for no FACTS device. The scope is always there to add new devices. The last value represents the rating of each FACTS device. This value is between  $-1$  and  $+1$ .  $-1$  corresponding to the minimum value that the device can take and  $1$  to the maximum.

TCSC:

By modifying the reactance of the transmission line, the TCSC acts as the capacitive or inductive compensation respectively. In this study, the reactance of the transmission line is adjusted by TCSC directly. The rating of TCSC is depends on the reactance of the transmission line where the TCSC is located:

$$\begin{aligned} X_{ij} &= X_{Line} + X_{TCSC}, \\ X_{TCSC} &= r_{tcsc} * X_{Line} \end{aligned} \quad (8)$$

Where  $X_{Line}$  is the reactance of the transmission line where the TCSC is placed and  $r_{tcsc}$  is the coefficient which represents the degree of compensation by TCSC. TCSC has a working range between  $-0.7X_{Line}$  and  $0.2X_{Line}$ .

SVC:

The SVC can be operated as both inductive and capacitive compensation. It is modeled as an ideal reactive power injection at bus  $i$ . The value is between  $-100$  MVAR to  $100$  MVAR.

$$\Delta Q = Q_{svc} \quad (9)$$

### 3.2 Reproduction

The Objective function is calculated for each generation and the fitness value is calculated to find the fitness of each individual. The individual is selected to for the new generation based on fitness.

### 3.3 Crossover

The crossover is done to rearrange the information of two individuals to produce new ones. Two point crossover is used here.

### 3.4 Mutation

Mutation is used to introduce some sort of artificial diversification in the population to avoid premature convergence before the local minima.

## IV. Simulation Results

In order to test the activeness of propound technique the modified IEEE 30 bus system without shunt capacitors is used shown in Fig 10. GA parameters for single objective optimization are

Population Size: 40, maximum no of generations: 200, crossover probability: 0.95: mutation probability: 0.001: and elitism index: 0.15

Different operating conditions are simulated to check the validity of proposed algorithm to find out the optimal location. The study considers three cases, BL as objective, VS as objective and Loss minimization as objective with base case and 130% loading with and without FACTS.

Comparative analysis of results with base case is tabulated. Base case here refers to load flow solution without any optimization objective. Fifteen runs are performed and the results presented are the best out of 15.

Table 1: Objective Function values with 130% loading

Objective Function	Base case	130% loading with FACTS devices		
		BL objective	VS objective	LM objective
Branch Loading (BL)	2537.32	<b>2837.109</b>	2289.215	2145.3538
Voltage Stability (VS)	1310.25	1329.838	<b>1389.583</b>	1023.693
Loss minimization	0.190	0.210	0.193	<b>0.179</b>

Table 1 indicates the objective function values for three objectives optimized individually for base load and 130% loading. It is clear that that with BL as objective the value has increased by 11.8% from base

case and with VS as objective the Value of VS function has increased by 14.2% and with LM as objective LM function has reduced by 6%.

4.1 Branch Loading Objective

Taking branch loading as the objective function the type, location and rating of TCSC and SVC is determined and the best solution obtained as shown in Table 2. Fig 2 and Fig 3 shows the graph of error Vs no. of generations and objective function value Vs no of generation.

Table 2: Optimized type, location and rating of FACTS devices for BL as objective at 130% loading loading

Type of device	Location	Rating
SVC	25	-0.005275
TCSC	Line 40	-0.11868

Table 3: Lines to be overloaded with 130 % loading with and without FACTS

Line No.	From Bus	To Bus	Spq in Base case	Spq in 130% loading	Spq After including FACTS devices	Spq max Through lines	Line loading in Base case	Line loading with 130% loading	Line loading after including FACTS devices
1	1	2	1.0944	1.6385	1.2356	1.3	84.183	126.036	95.046
2	1	3	0.4955	0.777	0.7682	1.3	38.117	59.7715	59.6655
3	2	4	0.3065	0.429	0.4194	0.65	47.1559	65.9961	66.1008
4	3	4	0.4597	0.7135	0.7121	1.3	35.3577	54.8819	54.7769
5	2	5	0.6062	0.8657	0.8524	1.3	46.6276	66.5947	66.5276
6	2	6	0.3857	0.5667	0.5592	0.65	59.3388	87.1786	87.579
7	4	6	0.3862	0.6189	0.6226	0.9	42.9084	68.7635	69.8429
8	5	7	0.1864	0.272	0.1616	0.7	26.6318	38.8503	37.7972
9	6	7	0.3577	0.4748	0.4675	1.3	27.5151	36.525	36.4473
10	6	8	0.1638	0.3551	0.3132	0.32	51.1727	110.97	97.875
11	6	9	0.1446	0.2328	0.2207	0.65	22.2527	35.8213	34.5275
12	6	10	0.1831	0.2391	0.1692	0.32	57.2275	74.713	72.1731

Table 3 indicates that the lines 1 and 10 are overloaded without the introduction of FACTS devices and the line loading has been decreased appreciably and power flow is also within limits with the optimal insertion of FACTS devices.

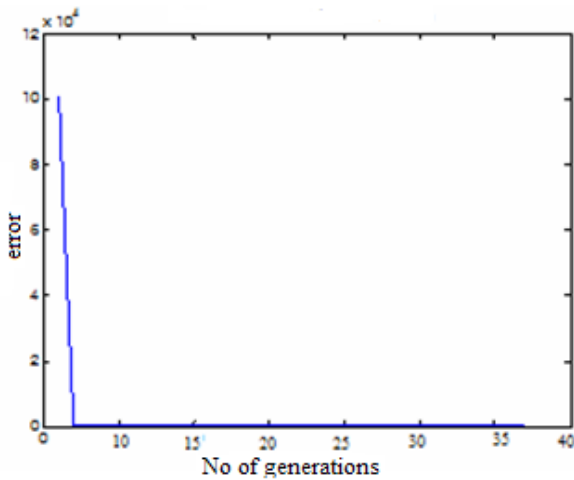


Fig. 2: Error Vs no. of generations

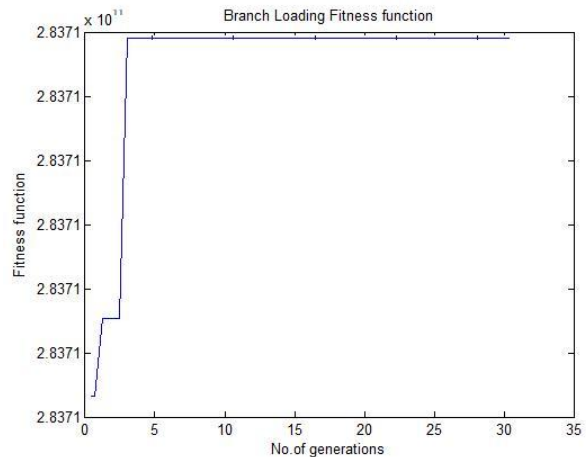


Fig. 3: Objective function Vs Generations

4.2 Line Outage

Line 5 outage

With the line 5 outage is there, the lines 6 and 8 are loaded by 105.4285% and 117.7534% respectively. This overloading can be relieved by placing SVC at 11<sup>th</sup> bus with Bsvc of -0.375057 and three TCSC devices in lines 14,23 and 11 with X<sub>TCSC</sub> of -0.080656,-0.008245 and -0.024216 respectively. Table 4 shows the comparative analysis of objective function values with

base case and with optimization. Fig 4 shows the error and generation graph and Fig 5 shows the graph between fitness value Vs generation.

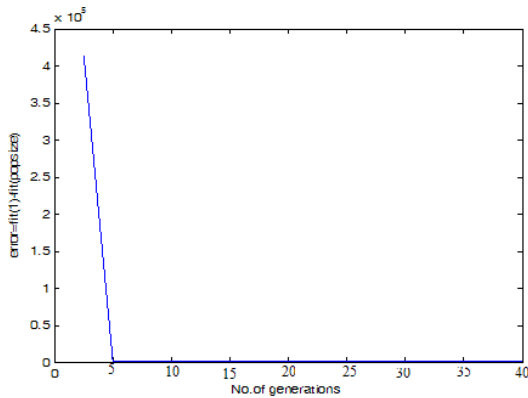


Fig. 4: Error Vs Generations with line 5 outage

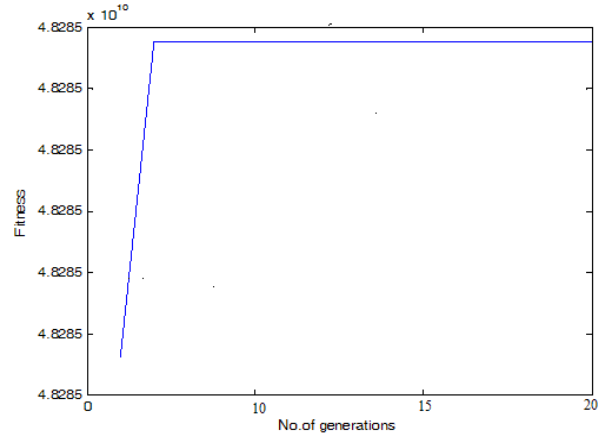


Fig. 5: Fitness Vs Generation with BL as objective

Table 4: Comparison of objective function values when line 5 given outage with and without FACTS devices at 130% loading

Objective Function	Base case	130% loading with FACTS devices		
		BL objective	VS objective	LM objective
Branch Loading (BL)	25.0162	<b>482.06</b>	486.112	483.393
Voltage Stability (VS)	121.1703	242.7302	<b>314.50</b>	248.74
Loss minimization	0.1691	0.170	0.170	<b>0.167</b>

#### Line 36 outage

When the line 36 given outage then lines 27, 30, 31 and 33 are loaded by 116.3357%, 103.8337%, 117.1324% and 127.7935% respectively. This overloading can be relieved by placing SVC at 1<sup>st</sup> bus with  $B_{svc}$  of 0.244239 and two TCSC devices in lines 31

and 33 with  $X_{TCSC}$  of -0.346388 and -0.325978 respectively. Table 5 shows the comparison of objective function values with base case and with optimization. Fig 6. shows the graph of fitness Vs generations with BL as objective.

Table 5: Comparison of objective function values when line 36 given outage with and without FACTS devices at 130% loading

Objective Function	Line 36 is outage	Line 36 outage with FACTS devices		
		BL objective	VS objective	LM objective
Branch Loading (BL)	60.8893	621.8524	601.7279	612.98
Voltage Stability (VS)	183.7809	302.0251	309.2734	295.91
Loss Minimization	0.12553	0.128988	0.127814	0.1238

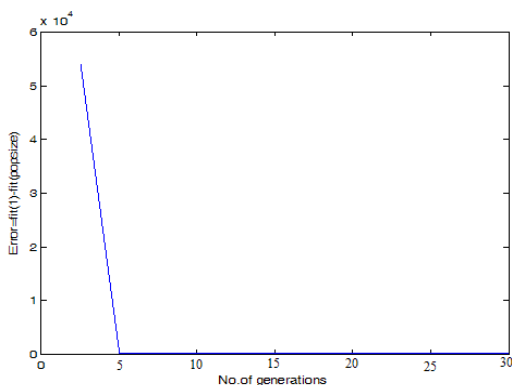


Fig. 6: Fitness Vs Generations

### 4.3 Voltage Stability as Objective

Taking voltage stability as the objective function the type, location and rating of TCSC and SVC is determined and the best solution obtained as shown in table 6. Fig 7 shows the graph of objective function and no of generation and Fig 8 indicates the graph of error of 1<sup>st</sup> and last generation and no of generations and with FACTS controller at optimal location. Table 7 shows the improvement in voltage profile of weak buses with the insertion of SVC at location 18 with rating -0.2668.

Table 6: Optimized type, location and rating of FACTS devices for VS as objective function at 130 % loading

Type of device	Location	Rating
SVC	18	-0.2668

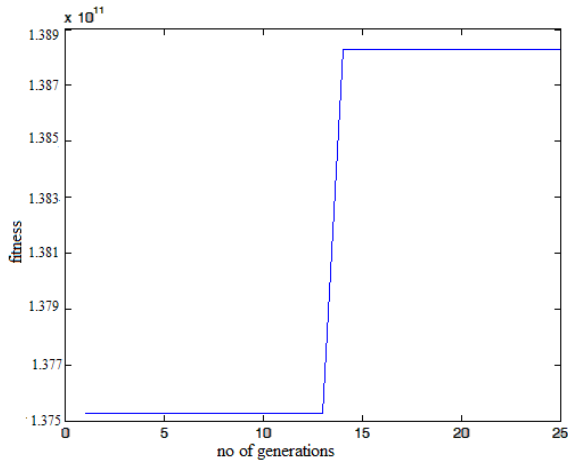


Fig. 7: Objective functions versus no of generation

Table 7: Voltage profile with FACTS

Bus No	Without facts at 130%loading	With TCSC and SVC at optimal location
26	0.8921	0.95366
30	0.8902	0.95909
21	0.9171	0.978

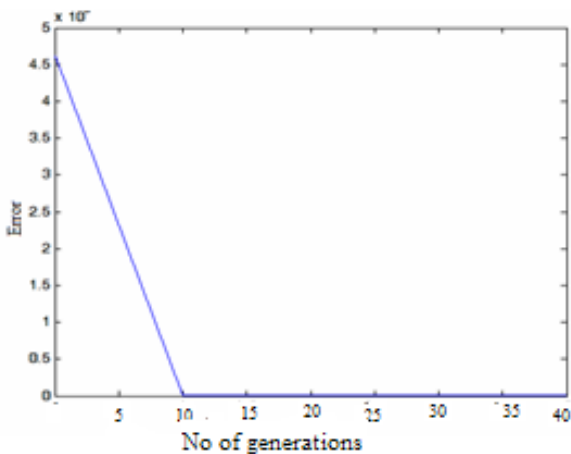


Fig. 8: Error versus no of generation for voltage Stability as objective

**4.4 Loss Minimization as Objective**

Taking Loss minimization as the objective function the type, location and rating of TCSC and SVC is determined and the best solution obtained as shown in table IX. Fig 9 shows the error between fitness value of 1<sup>st</sup> iteration and last iteration. Table VIII shows the active and reactive losses with FACTS controller.

Results indicate that by proper placement of FACTS devices, losses are reduced considerably.

Table 8: Power loss at 130 % loading

Active power loss without FACTS	Reactive loss without FACTS	Active loss with FACTS	Reactive loss with FACTS
0.181	0.495	0.179	0.4007

Table 9: Optimized type, location and rating of device at 130% loading with loss minimization as objective

Type of device	Location	Rating
TCSC	22	0.03387

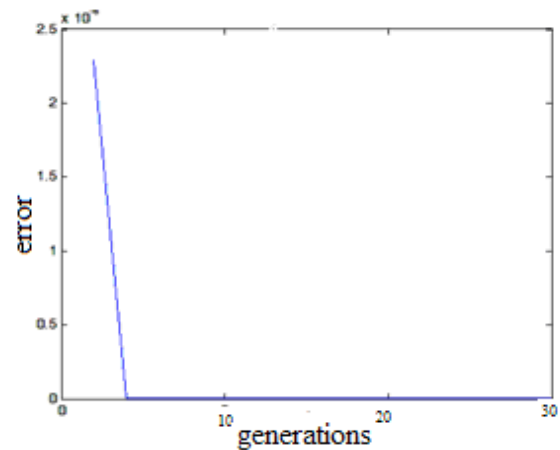


Fig. 9: Error Vs No of generation

**V. Conclusion**

Taking Loss minimization as the objective function the type, location and rating of TCSC and SVC is determined and the best solution obtained as shown in table IX. Fig 9 shows the error between fitness value of 1<sup>st</sup> iteration and last iteration. Table VIII shows the active and reactive losses with FACTS controller. Results indicate that by proper placement of FACTS devices, losses are reduced considerably.

**Acknowledgments**

The authors would like to thank the anonymous reviewers for their careful reading of this paper and for their helpful comments.



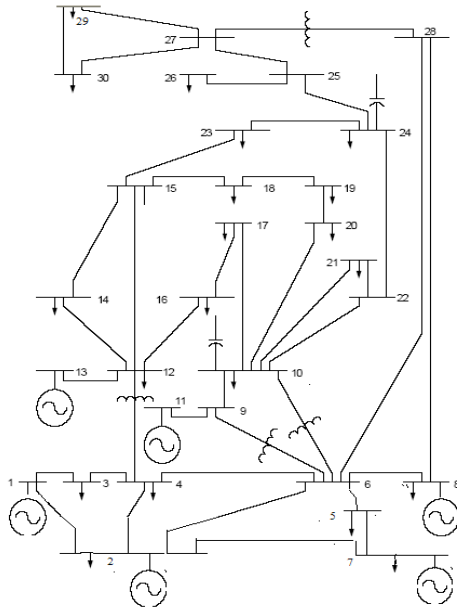


Fig 10: IEEE 30 bus system

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